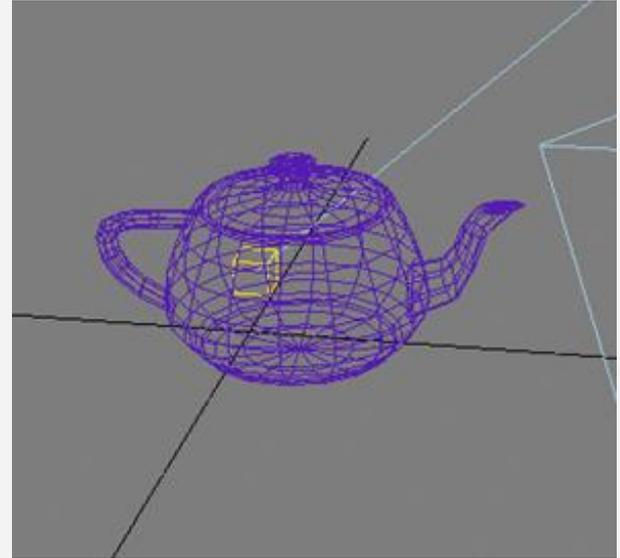


# Recollection



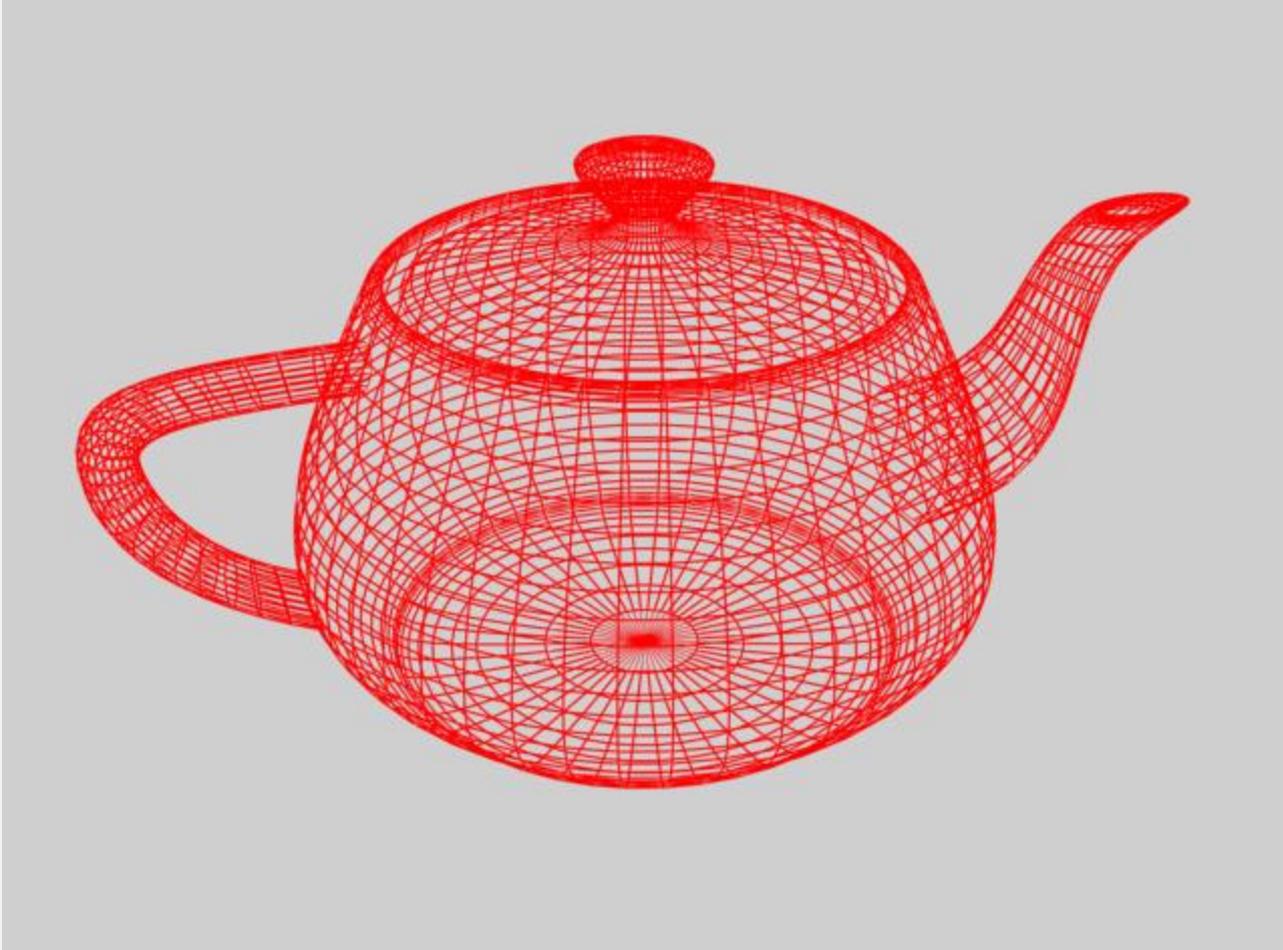
- Models → Pixels
- Model transformation
- Viewport transformation
- Clipping
- Rasterization
- Texturing
- + Lights & shadows
  - Can be computed in different stages





So far we came to...

# Geometry model



# Surface color



# Now: Shading





**Important  
recollections**

# Bilinear interpolation

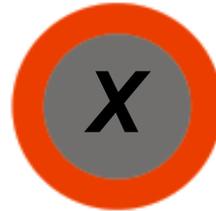


**A**



**D**

**P**



**Q**

**B**



**C**

# Bilinear interpolation



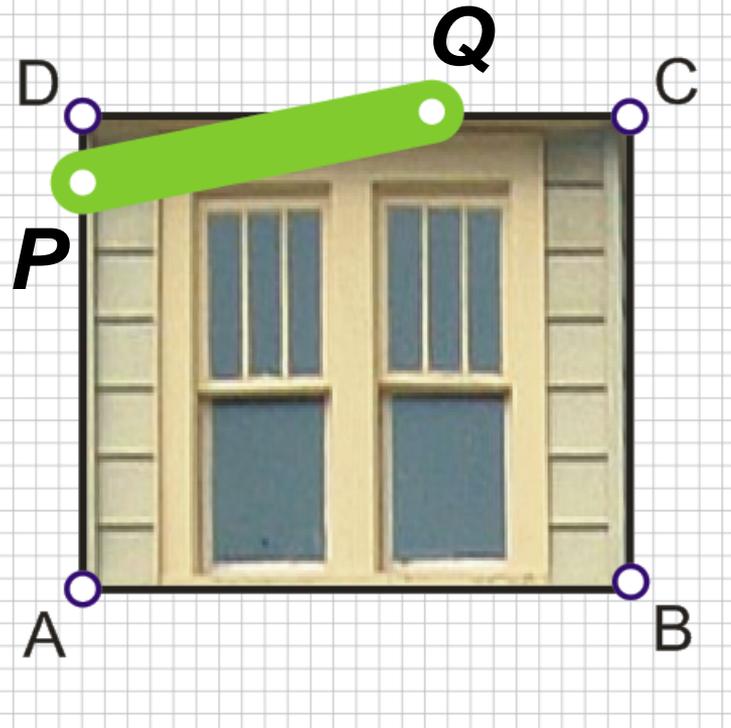
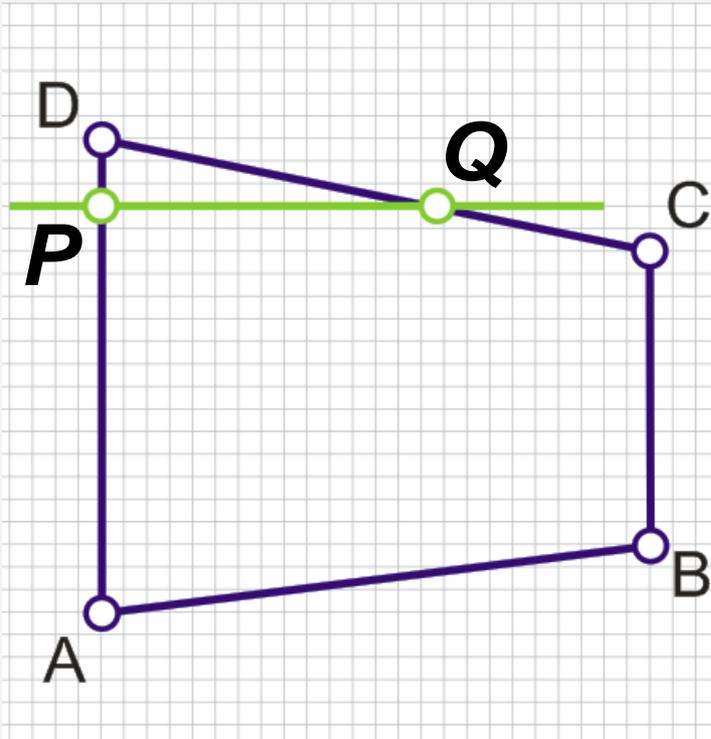
- 4 corner points  $A, B, C, D$  with known values
- 1 internal point  $X$  with unknown value
- $P = A + u.(B-A), Q = D + u.(C-D)$
- $X = P + v.(Q-P)$
  
- Matrix representation

$$X = (1-u, u) \begin{pmatrix} A & D \\ B & C \end{pmatrix} \begin{pmatrix} 1-v \\ v \end{pmatrix} \quad u \in \langle 0, 1 \rangle, v \in \langle 0, 1 \rangle$$

# Application: texture mapping



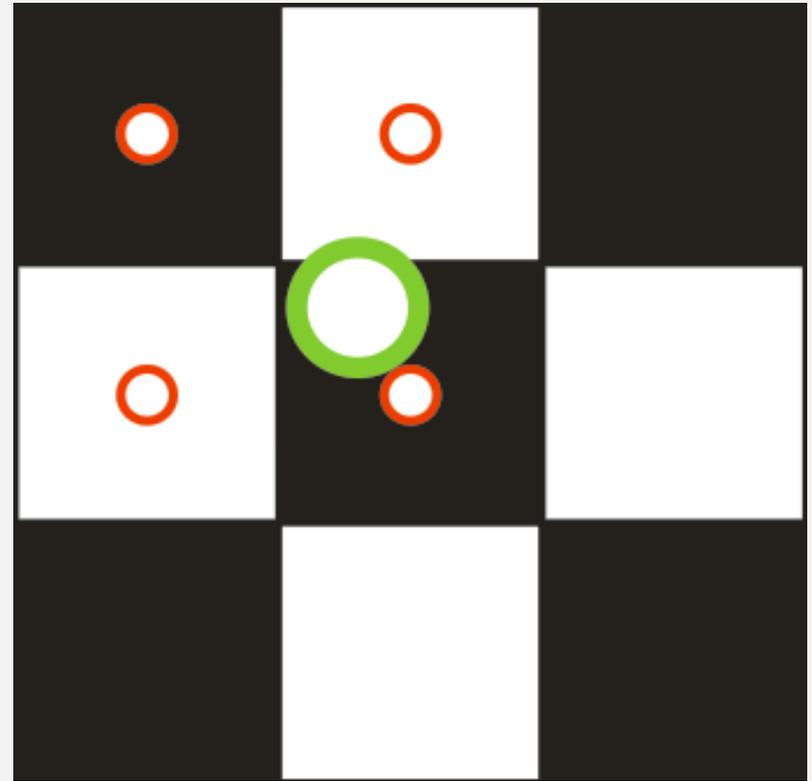
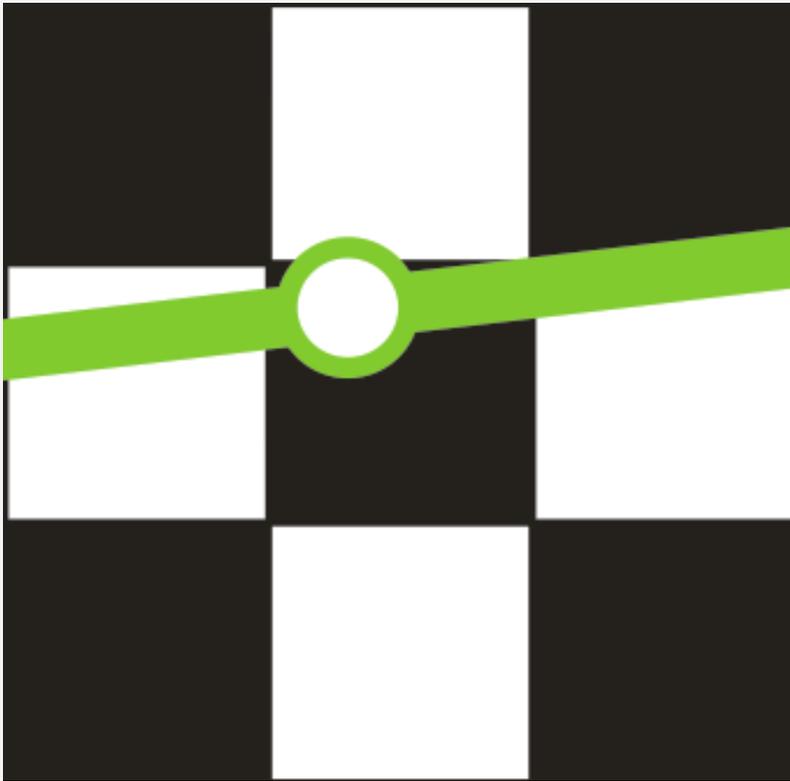
- Interpolate  $D \leftrightarrow A = P$ ,  $D \leftrightarrow C = Q$ ,  $P \leftrightarrow Q = X$



# Application: texture filtering



- Consider 4 neighboring texels
- Weighted average





# Lighting and shading

# General problem



- For a point in space, calculate lighting conditions and modulate the inherent object color to produce final pixel color



# Lighting and shading



- What is lighting
  - Computing amount of radiance (per wavelength) reflected from object towards the camera
- What is shading
  - Creating illusion of space in planar images
  - Usually uses lighting but other options are available too – e.g. depth shading



# Lighting

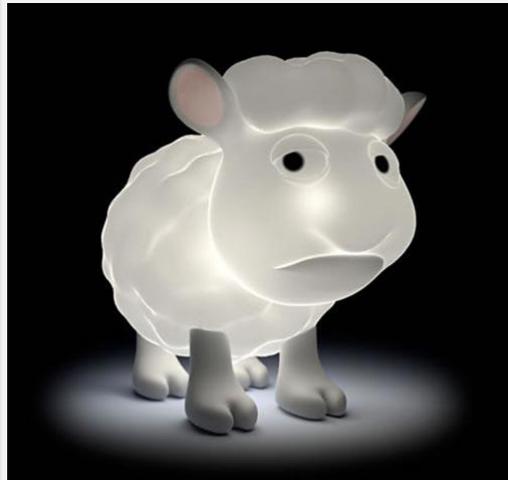
# Light source types



- Omnidirectional
- Spotlight
- Area
- Directional
- Object



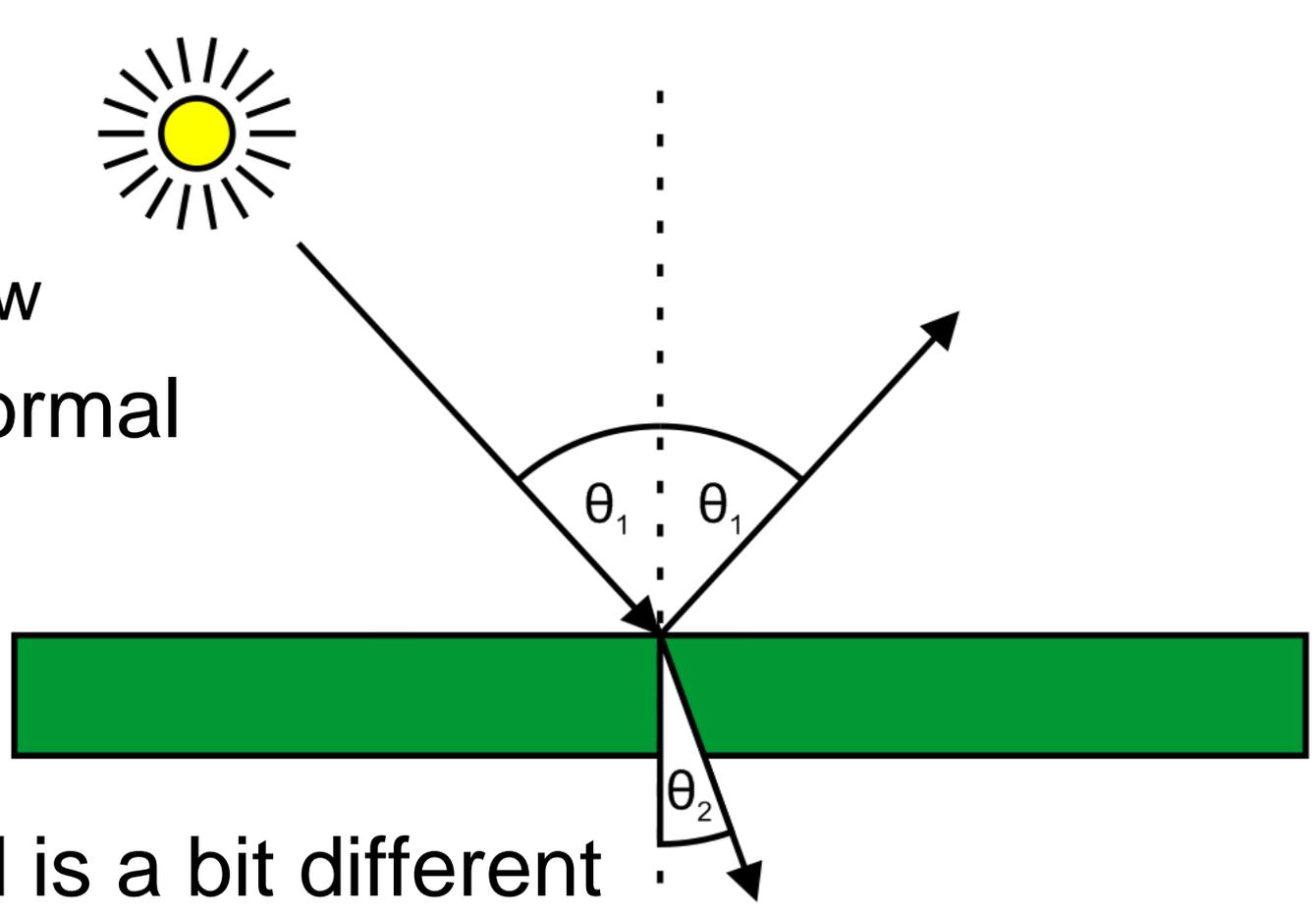
- what are the differences?



# Elementary theory



- Light-surface interaction
- Reflection
- Refraction
  - Snell's law
- Surface normal vector

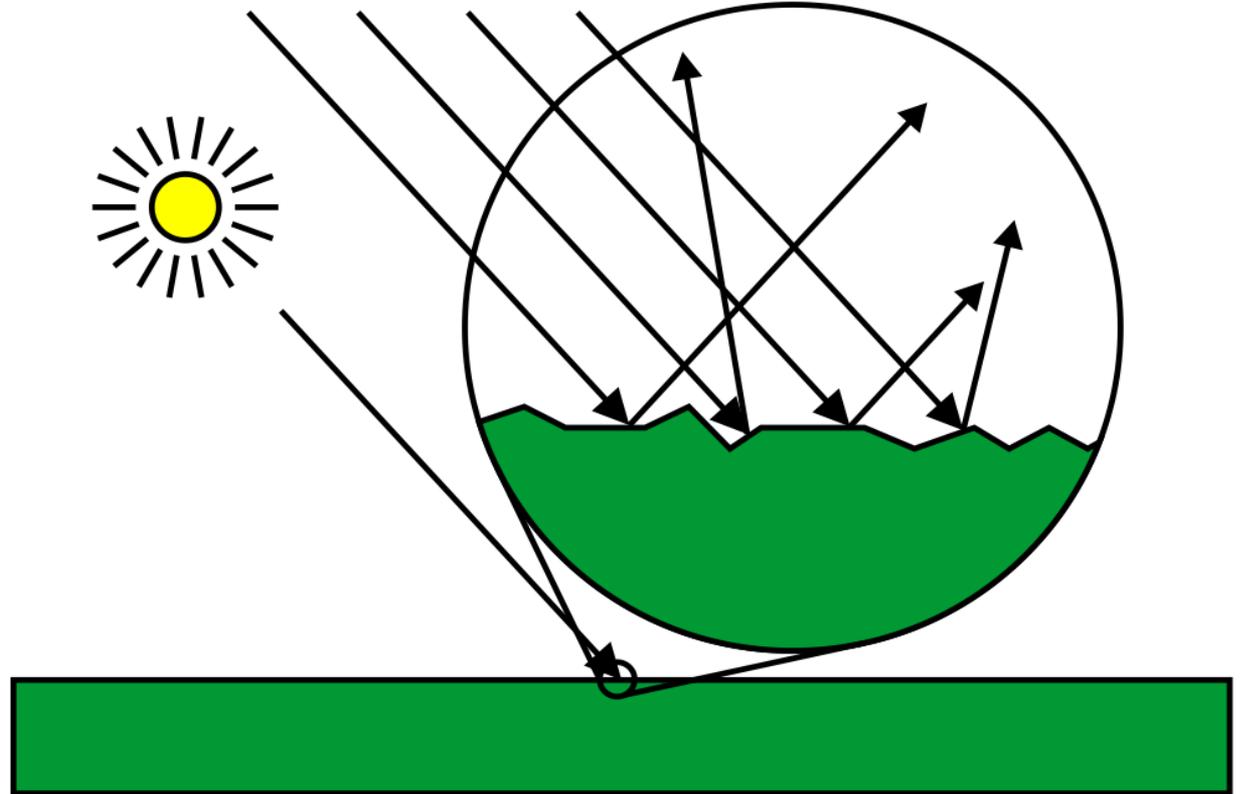


- Real world is a bit different

# Surface types



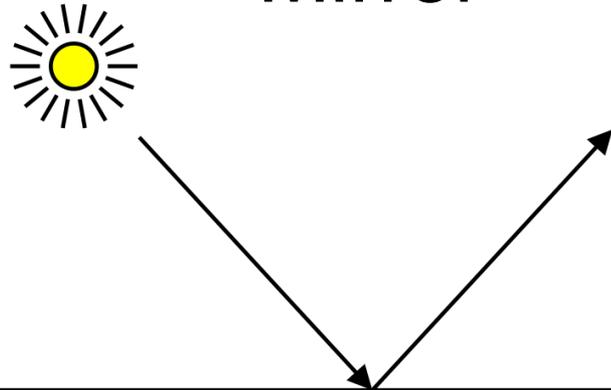
- Reflective
- Diffuse – Lambertian
- Both



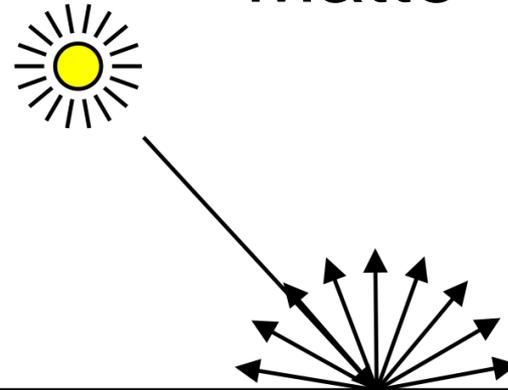
# Light reflection distribution



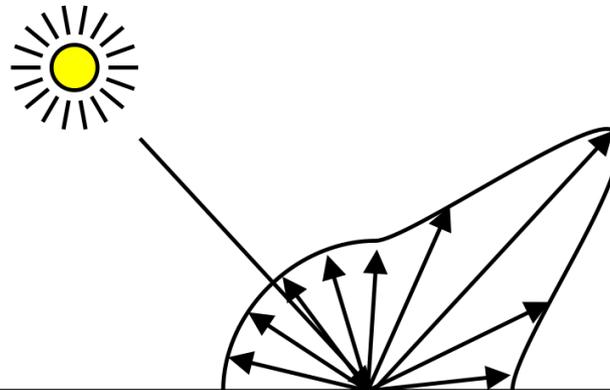
Mirror



Matte



directional  
component



indirectional  
component

# Lighting models



- Empiric – e.g. Phong lighting model
  - cheap computation
  - physically incorrect
  - visually plausible
- Physically-based
  - energy transfer, light propagation
  - closer to real-world physics
  - expensive

# Local illumination models

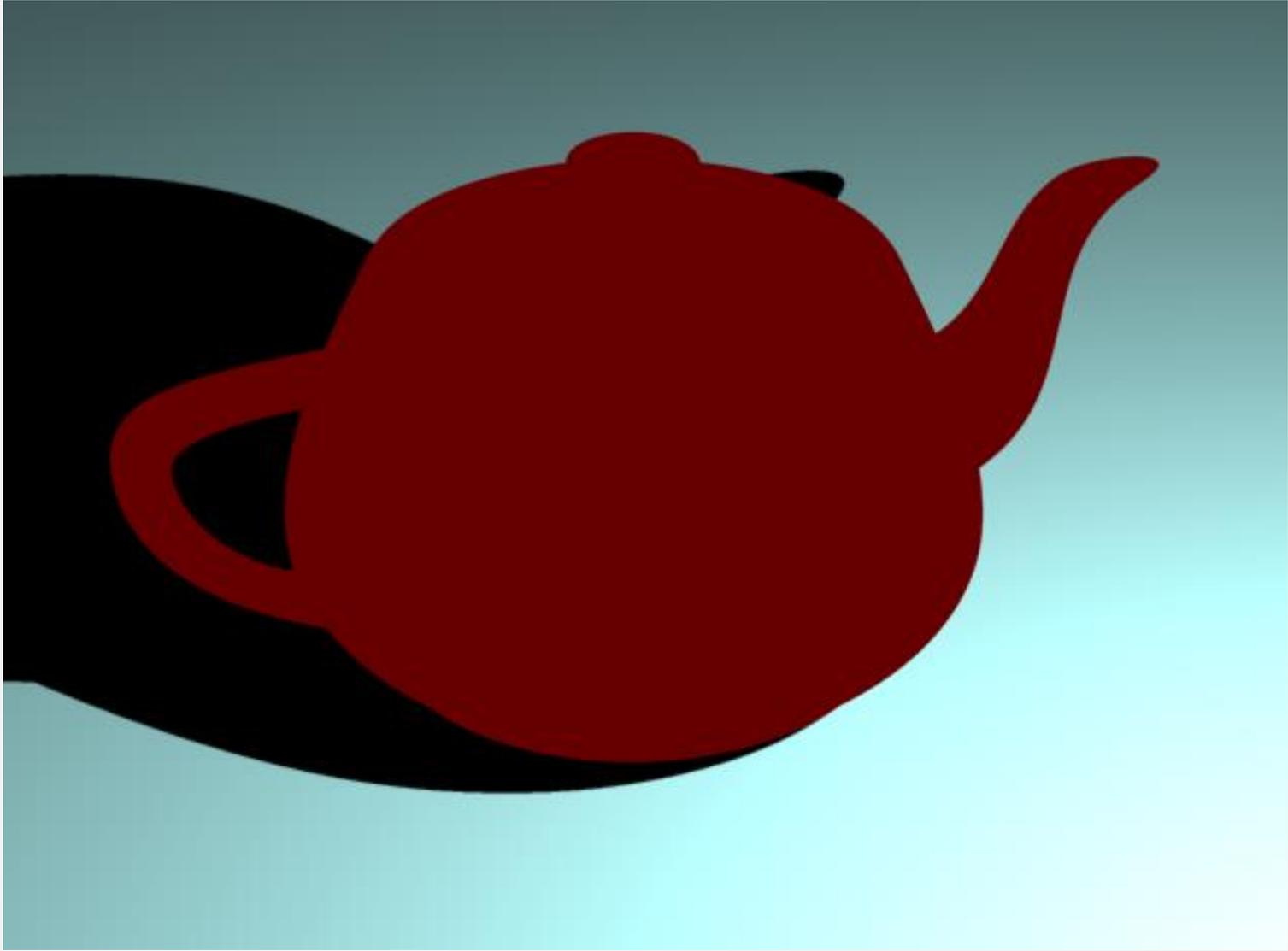


- Fast but inaccurate
- Ignore other objects (i.e. it's not global)
- Empirical (no physical background)
- Many physical effects are impossible to achieve
  
- Computer games, real-time rendering

# Diffuse light



# Ambient light



# Diffuse + ambient



# Diffuse + ambient + specular



# Phong lighting model



- **Ambient + Diffuse + Specular components**

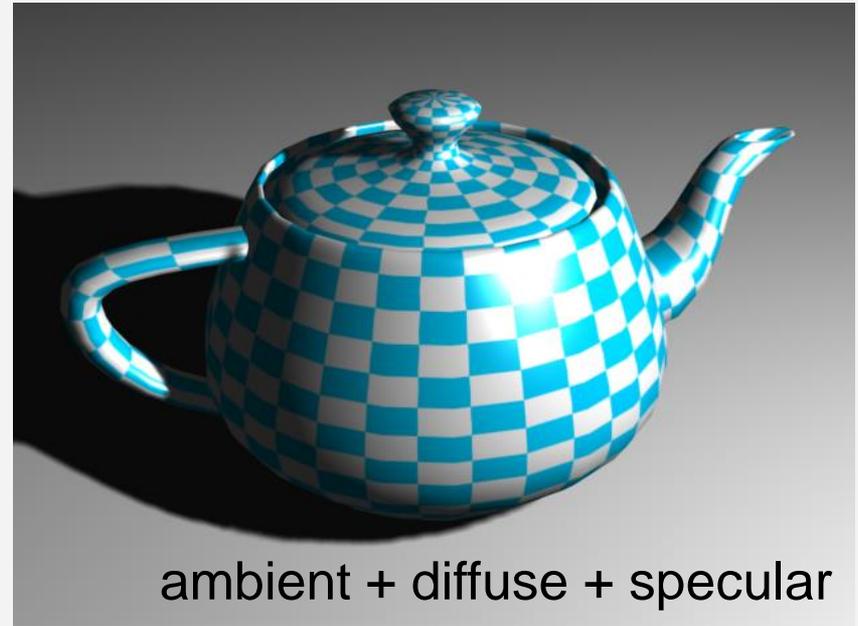
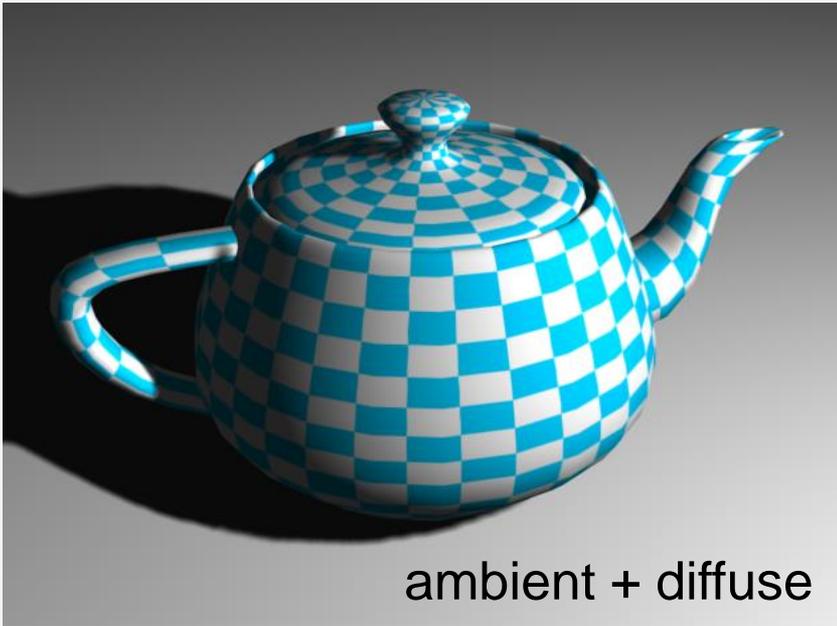


- Simulates global light scattered in the scene and reflected from other objects

# Phong lighting model



- Ambient + **Diffuse** + Specular components

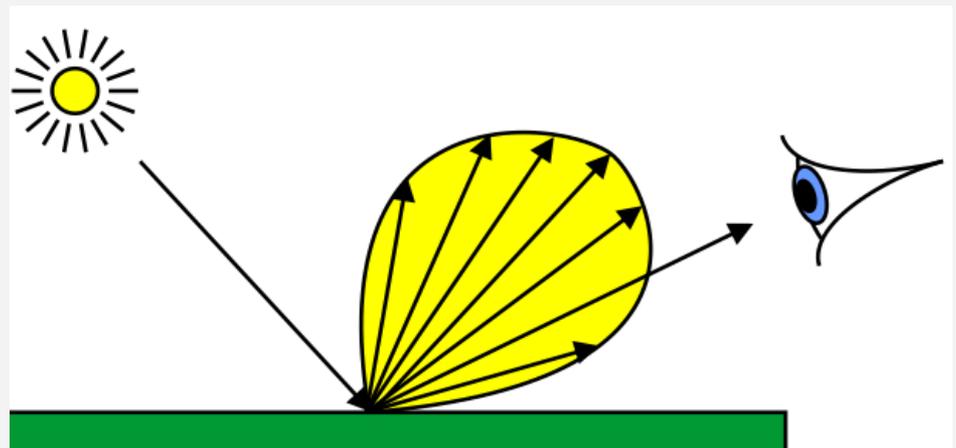
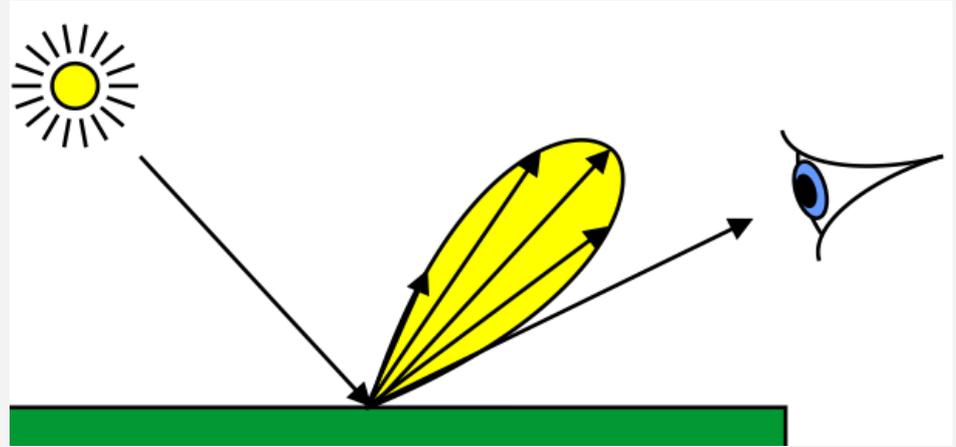


- Lambert law  $I_d = \vec{n} \cdot \vec{l}$

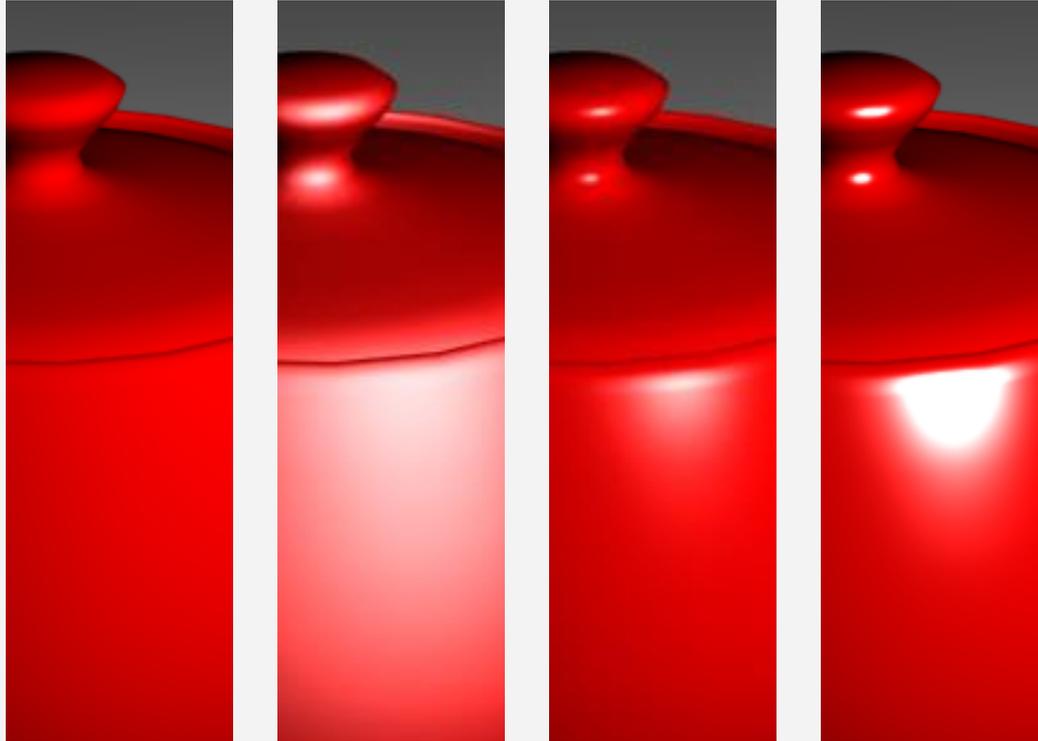
# Phong lighting model

- Ambient + Diffuse + **Specular** components
- Directional
  - view vector

$$I_s = (\vec{r} \cdot \vec{v})^{k_{shine}}$$



# Specular component



- $\mathbf{r} \cdot \mathbf{v} = |\mathbf{r}| \cdot |\mathbf{v}| \cdot \cos(\angle rv)$
- absolute parameter  $k_s$
- exponential parameter shininess (gloss)

# Phong lighting model



$$I = k_a I_a + \sum_{\forall \text{lights}} (k_d I_d + k_s I_s)$$

- $k, I$  coefficients can depend on wavelength
- what defines surface lighting properties?
  - $k_a, k_d, k_s, k_{\text{shine}}$

# Other lighting models

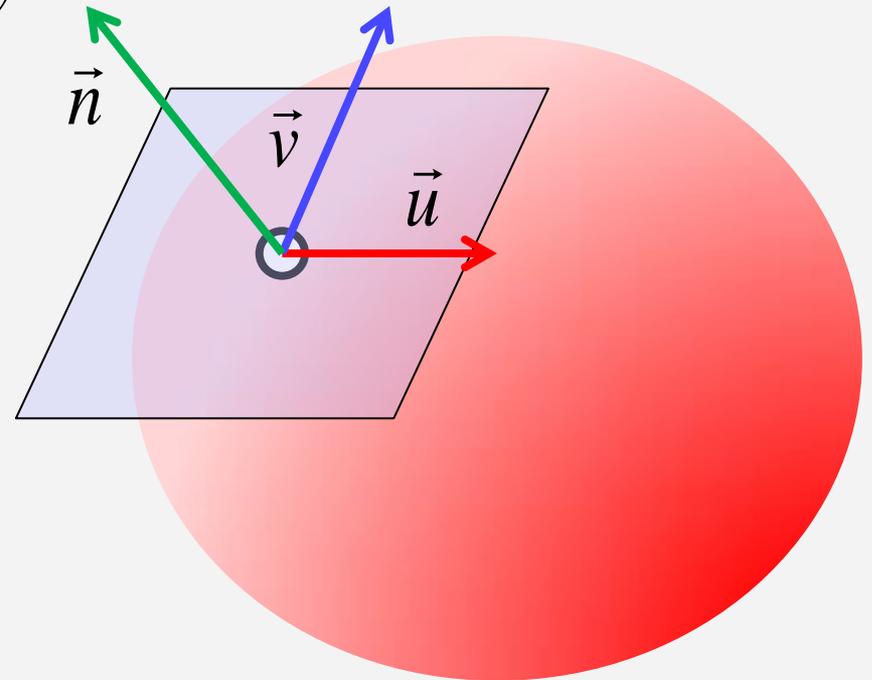


- Blinn-Phong
  - generalization of Phong's model
- Cook-Torrance
  - microfacets
- Oren-Nayar
  - rough surfaces
- Anisotropic microfacet distribution

# Surface normal vector



- Perpendicular to the surface at the point
- Computation:
  - Usually from tangent vectors
  - Vector product  $\vec{n} = \vec{u} \times \vec{v}$
  - Depends on the object representation



- Vector normalization  $\hat{n} = \frac{\vec{n}}{|\vec{n}|}$

# Tangent vectors

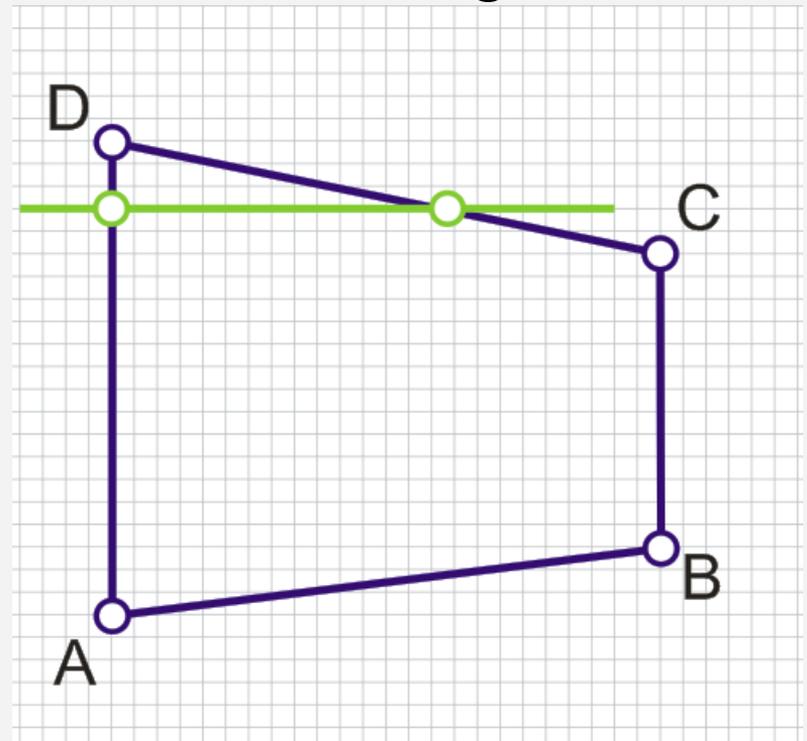


- Parametric representation
  - $X = x(u, v)$
  - $Y = y(u, v)$
  - $Z = z(u, v)$
  - Partial derivation by  $u, v \rightarrow$  vectors  $t_u, t_v$
- Polygonal representation
  - Tangent vectors are edge vectors
  - Mind the orientation!

# Lighting a polygon



- Scanline rasterization
- For each pixel – evaluate lighting model
  - compute normal vector, view vector, light vector
  - get surface parameters
  - evaluate formula
- Expensive
  - therefore: shading



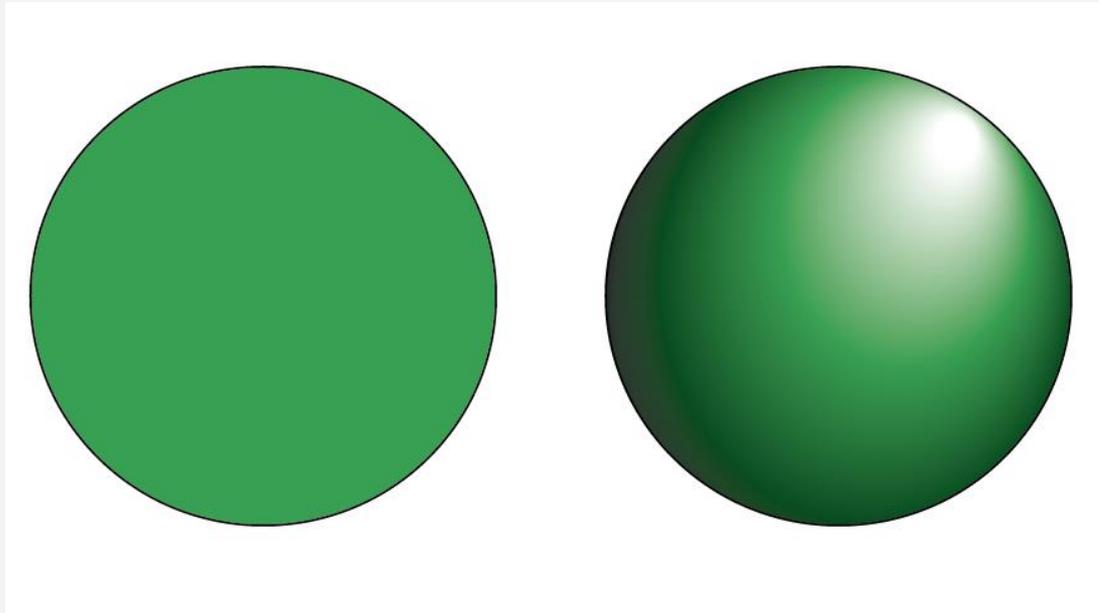


# Shading

# Shading



- Object color is altered to give impression of light and depth

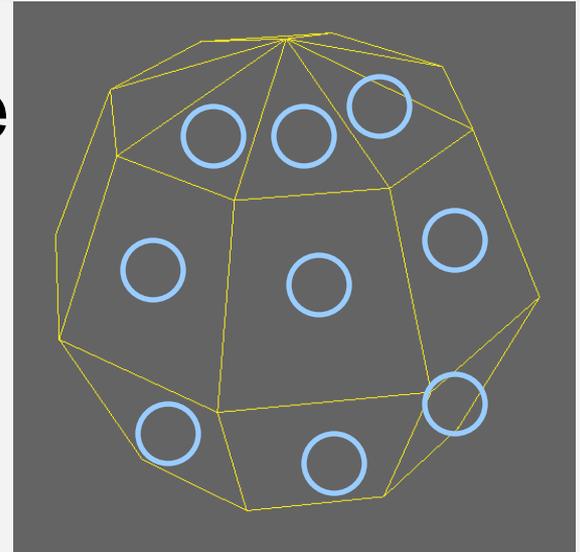


- Usually incorporates lighting
- Often only an approximation of real physics

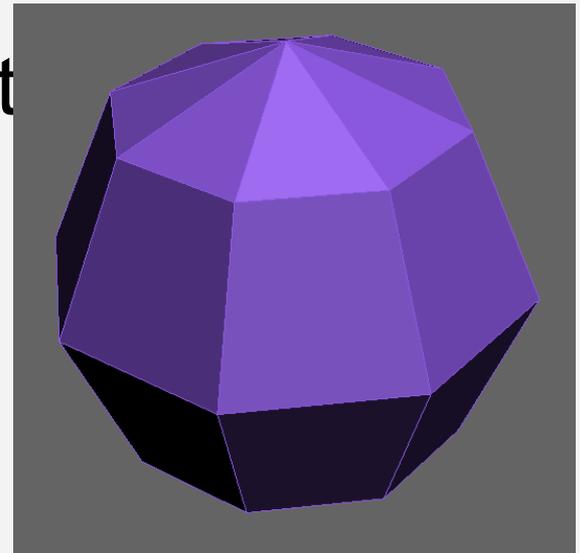
# Two stages of lighting



1. Evaluate illumination for some object  
**= LIGHTING**



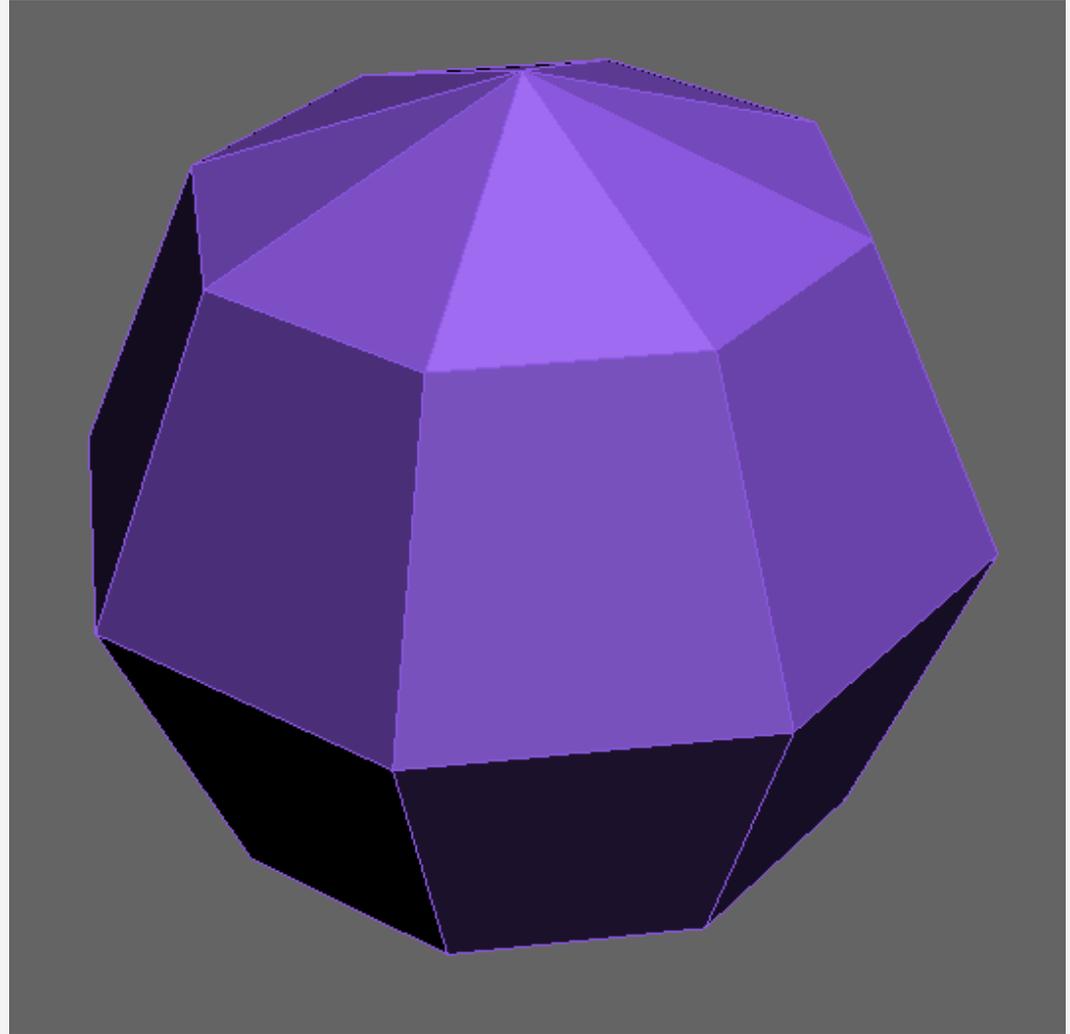
2. Use results from (1) to compute of the rest of the object  
**= SHADING**



# Flat shading



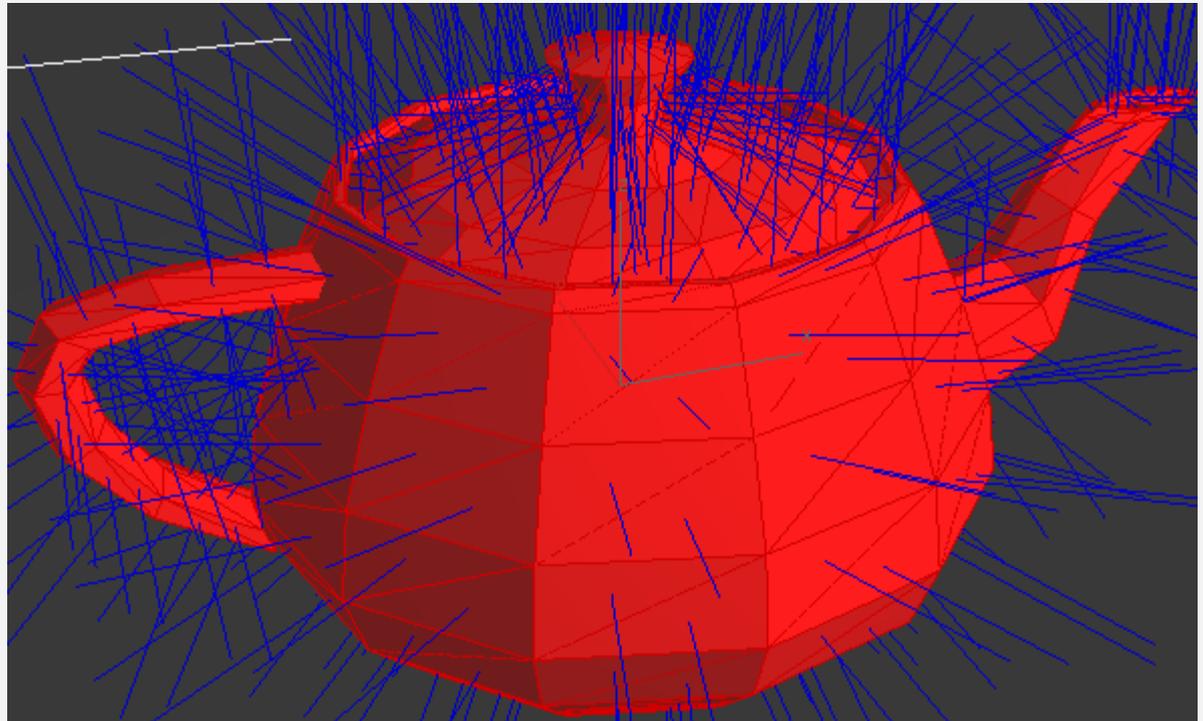
- One normal per face
- Entire face = one color



# Flat (constant) shading



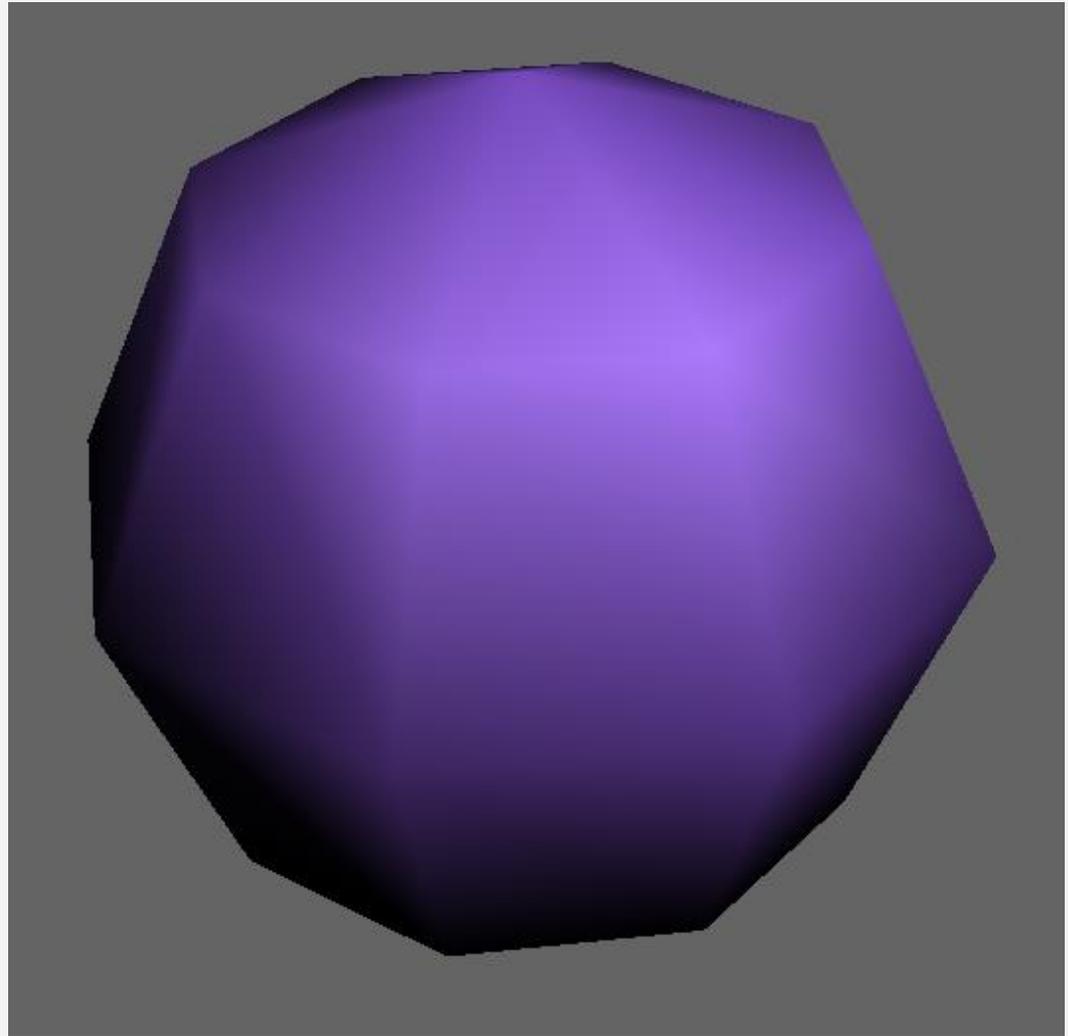
- 1 normal vector per object face (polygon)
- 1 lighting value per object face
- Entire polygon = 1 color



# Gouraud shading



- Per-vertex lighting
- Color is interpolated over the face



# Gouraud shading



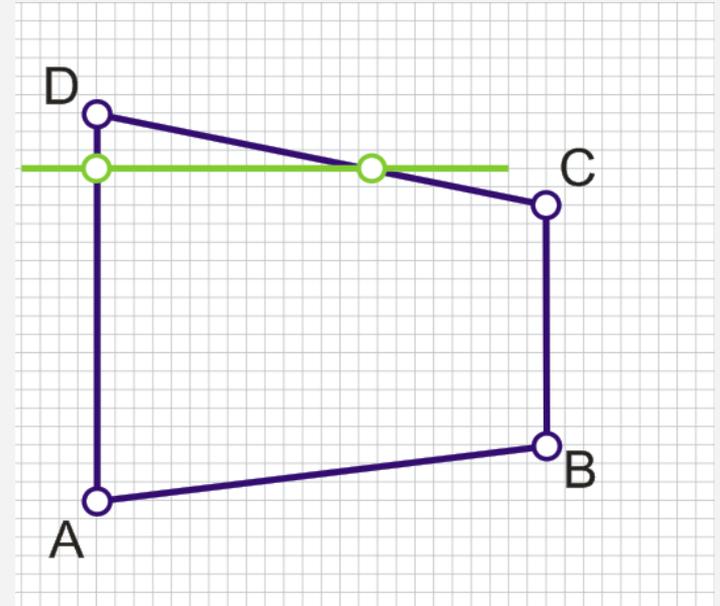
- 1 normal vector per 1 surface vertex
  - i.e. 4 lighting values / quad, 3 values / triangle
- Rest of the polygon – lighting value interpolation
- Bands
- Chance of missing specular
- Realtime



# Example



- $A[0, 0] = 80\%$  intensity
- $B[10, 6] = 20\%$
- $C[10, 9] = 80\%$
- $D[0, 10] = 40\%$



- Interpolate light intensity at  $S[5, 8]$
- HINT: Bilinear interpolation

$A \dots D \Rightarrow P$

$B \dots C \Rightarrow Q$

$P \dots Q \Rightarrow S$

# Phong shading



- NOT Phong lighting model
- Entire surface normal is interpolated instead of interpolating only the lighting value
- Per pixel lighting
- Slower



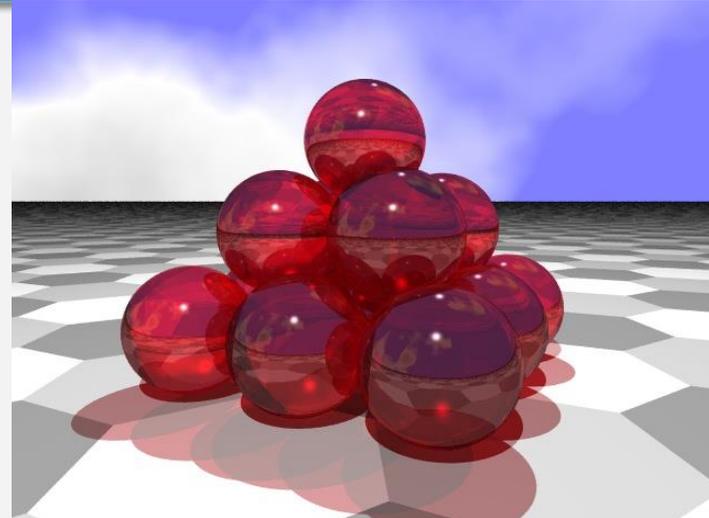


Towards photorealism

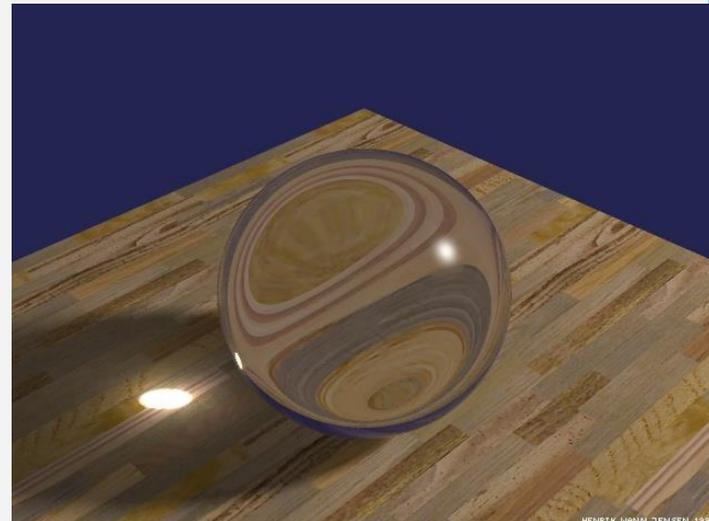
# Real world effects



- light refraction
- mutual object reflection
- caustics
- chromatic aberration
- color bleeding
- (soft) shadows

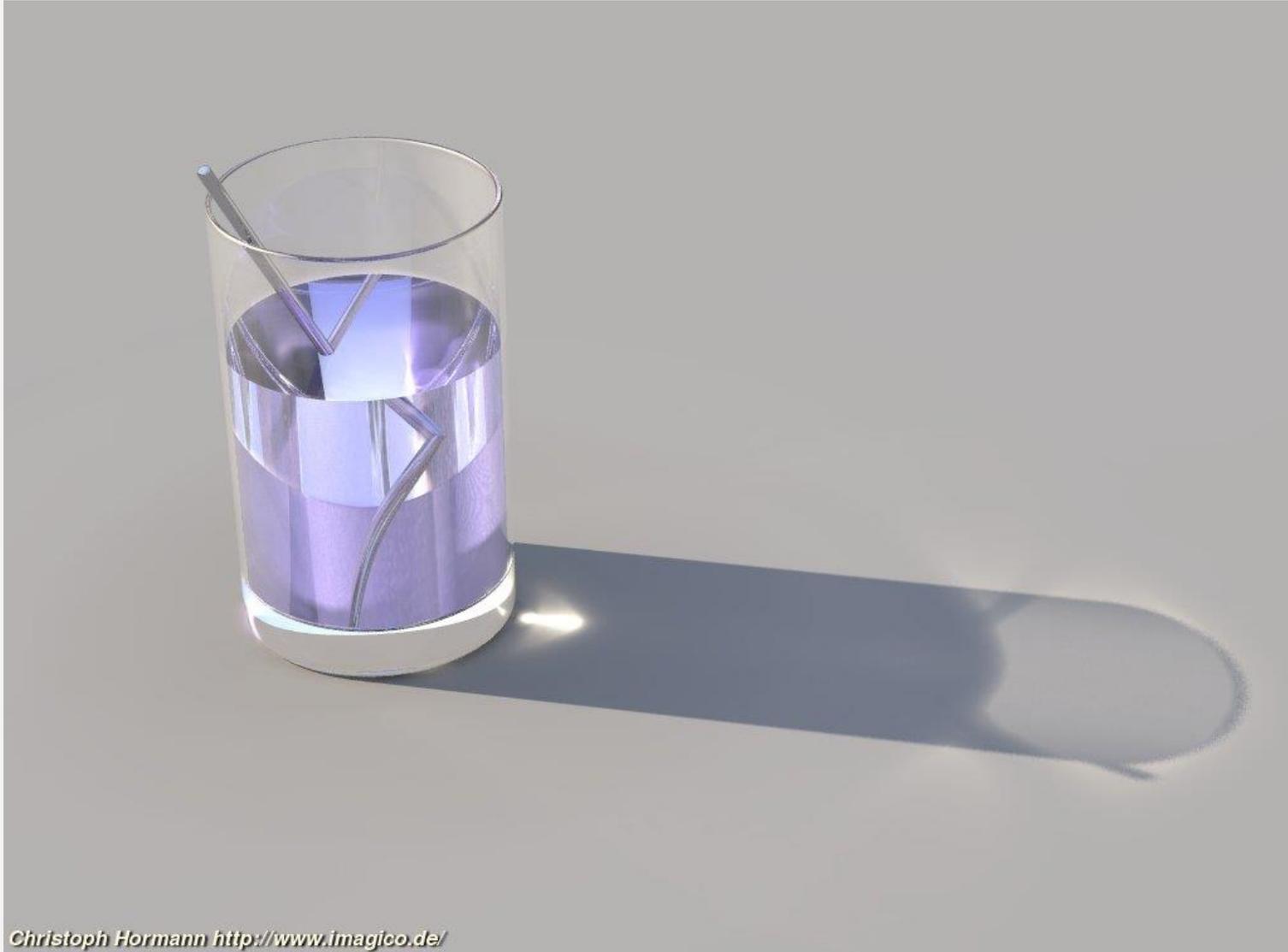


<http://math.hws.edu/eck>



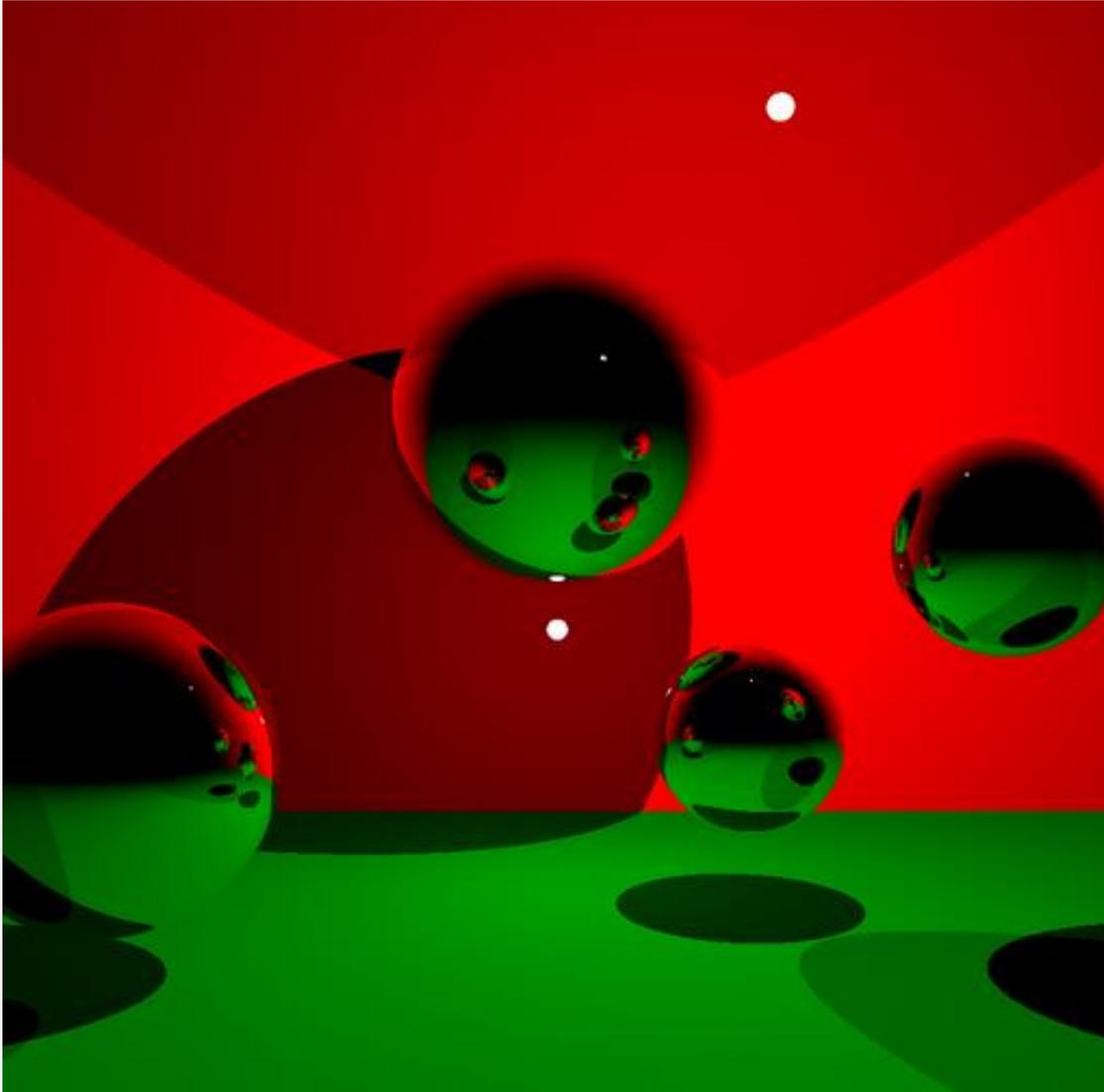
<http://graphics.ucsd.edu/~henrik/>

# Refraction, caustics



Christoph Hormann <http://www.imagico.de/>

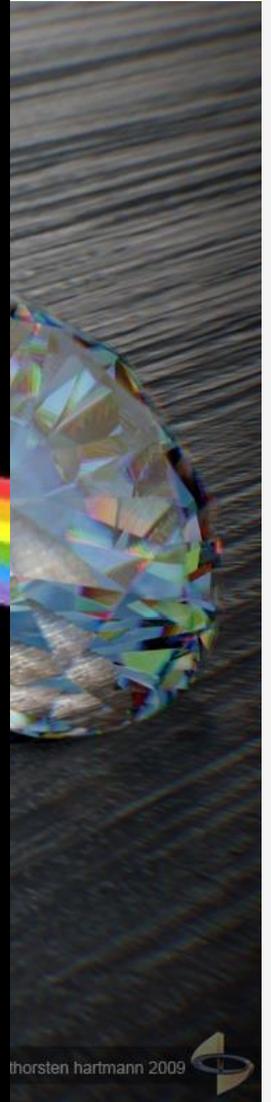
# Reflections



# Chromatic aberration

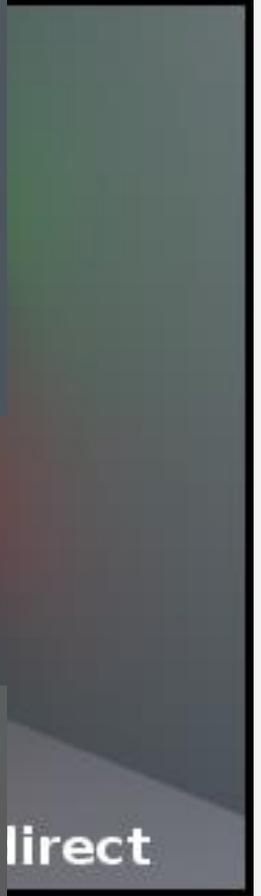
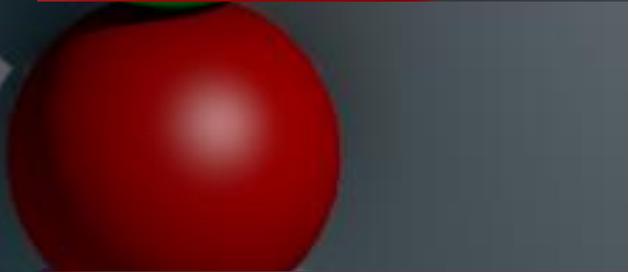


(Photo Studio Pro V3+ / Dispers



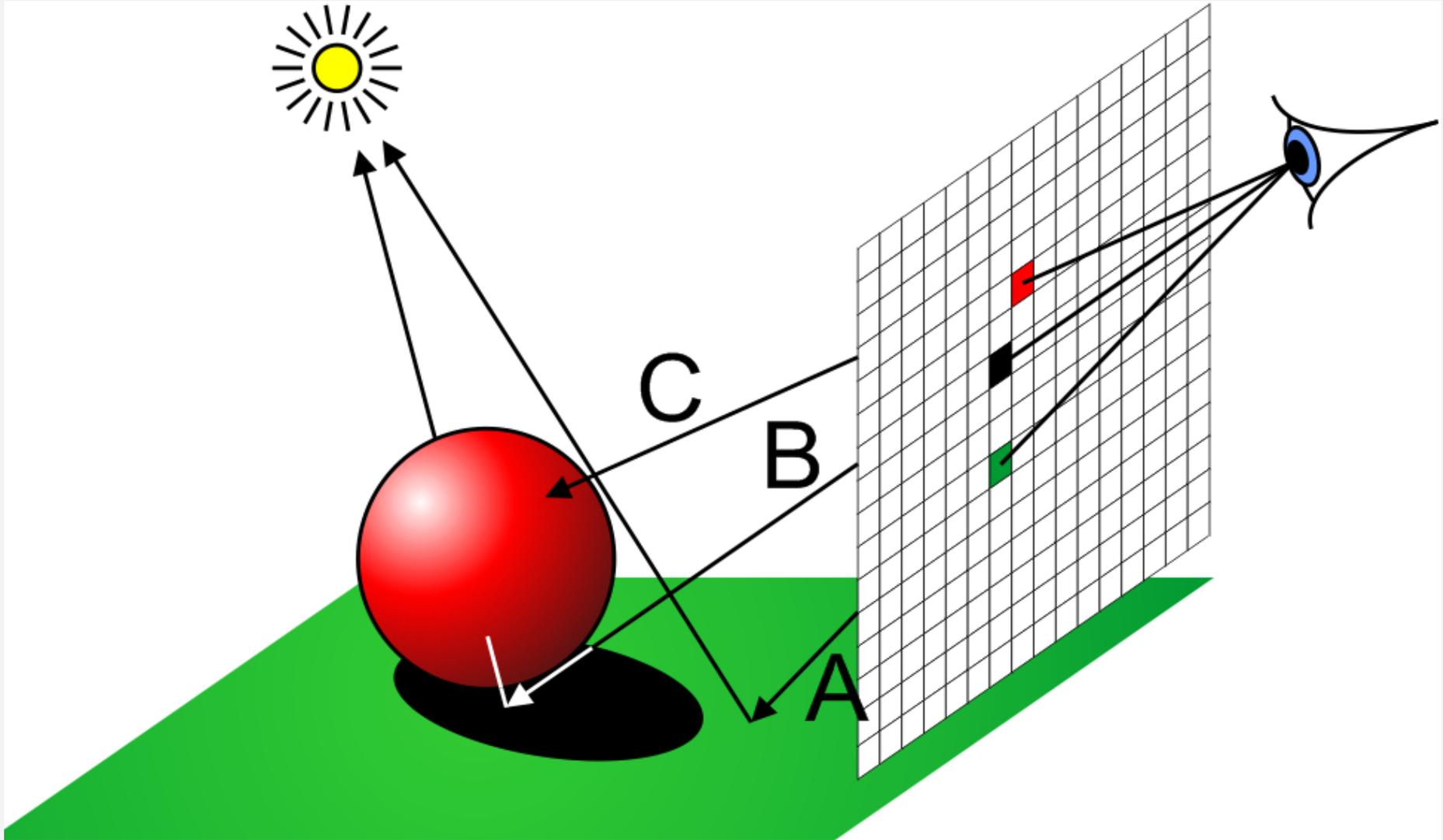
thorsten hartmann 2009

# Color bleeding



.org/blog/

# Raytracing



# Raytracing



- Tracing a beam from viewer's eye through each screen pixel.
- Find first beam intersection with objects
- Compute local lighting
- Trace reflected and refracted beams
- Combine the results with local result
  - recursively

# Raytracing – what's inside

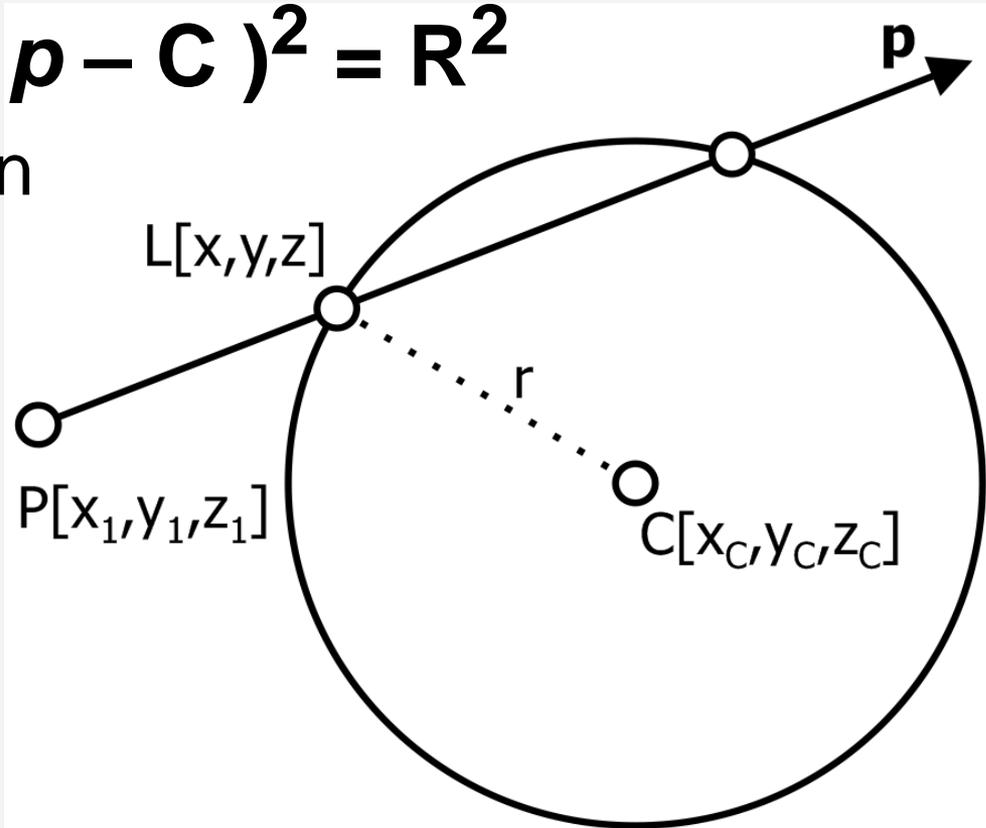


- Line-object intersection
  - expensive computation
  - speed-up by e.g. scene subdivision (octree) or bounding volumes
  - take the nearest intersection
- Example intersections:
  - Sphere
  - Triangle

# Line-sphere intersection



- Line  $A, p$  :  $L = P + t * p$
- Sphere  $C, r$  :  $(S - C)^2 = R^2$
- Intersect:  $(P + t * p - C)^2 = R^2$ 
  - Quadratic equation
  - 0, 1, 2 roots



# Line-triangle intersection

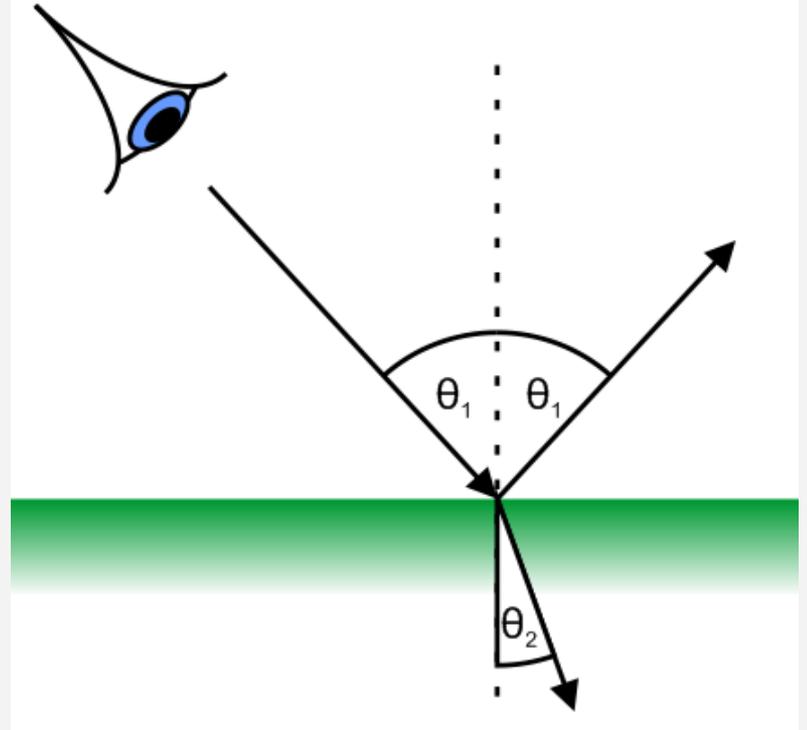


- Line  $P, p$  :  $\mathbf{L} = \mathbf{P} + t * \mathbf{p}$
- Triangle  $K, L, M$ :  $\mathbf{T} = \mathbf{K} + u*(\mathbf{L}-\mathbf{K}) + v*(\mathbf{M}-\mathbf{K})$
- Line-plane intersection
  - Plane:  $\mathbf{ax} + \mathbf{by} + \mathbf{cx} + \mathbf{d} = 0$
- Check if intersection is inside triangle

# Raytracing – what's inside



- Compute reflected and refracted rays
  - evaluate light coming from their direction
- Combine with the local lighting result



$$C = \text{comb}(l.C_L, r.C_R, t.C_T)$$

# Let's think the combinations



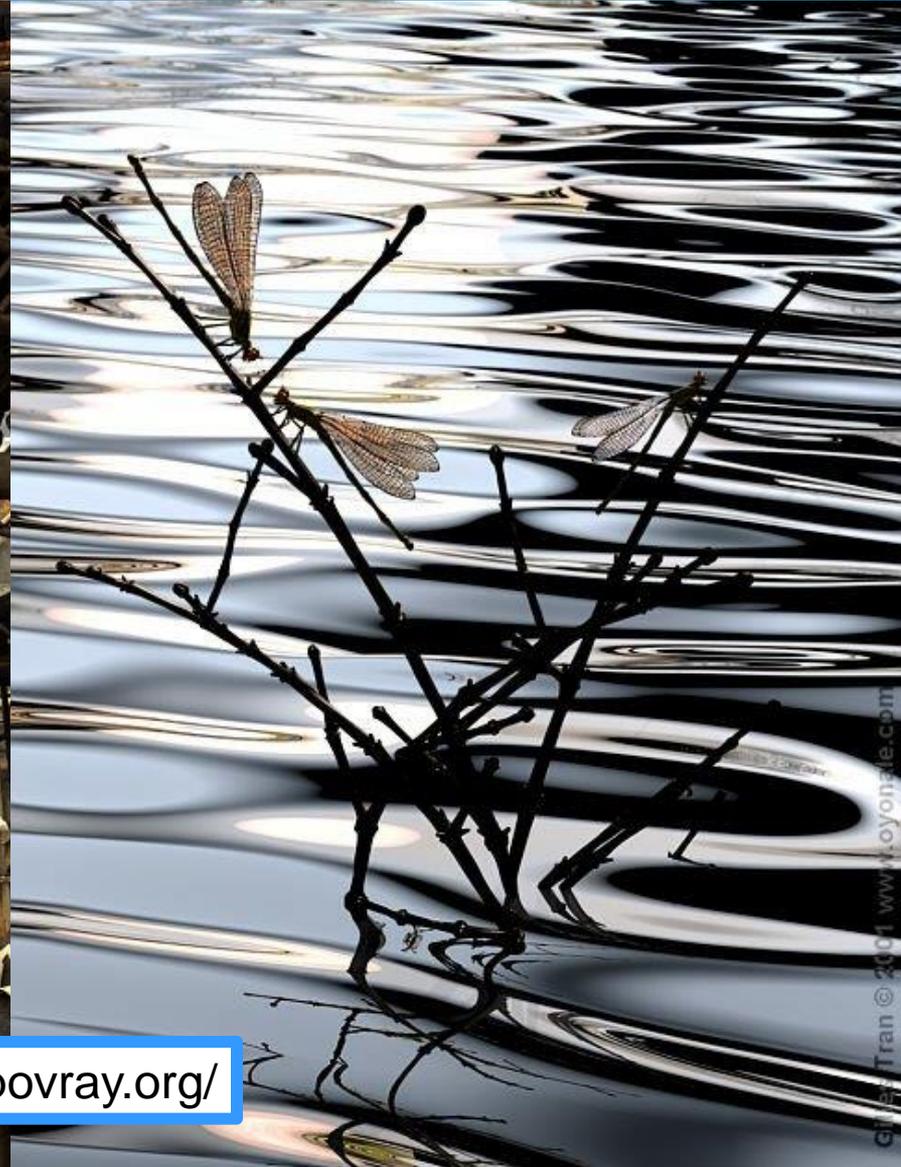
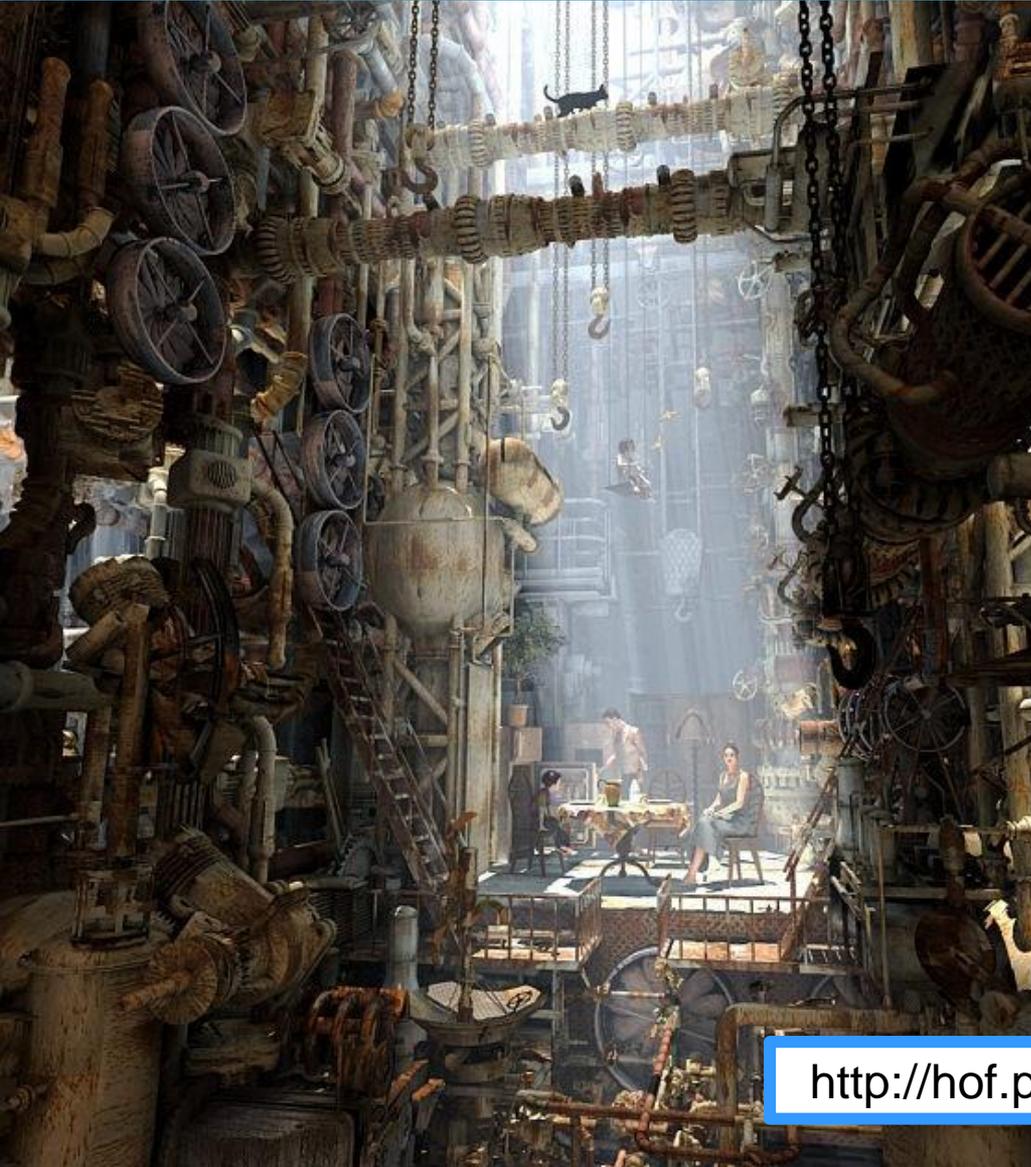
$$C = \text{comb}(l.C_L, r.C_R, t.C_T)$$

# Raytracing – pros and cons



- No need for polygonal representation
  - works with both volume and boundary rep.
  - works with CSG objects, F-reps, meshes...
- No explicit rasterization takes place
  
- Computationally expensive
- Does not compute soft shadows

# Examples: POV-Ray



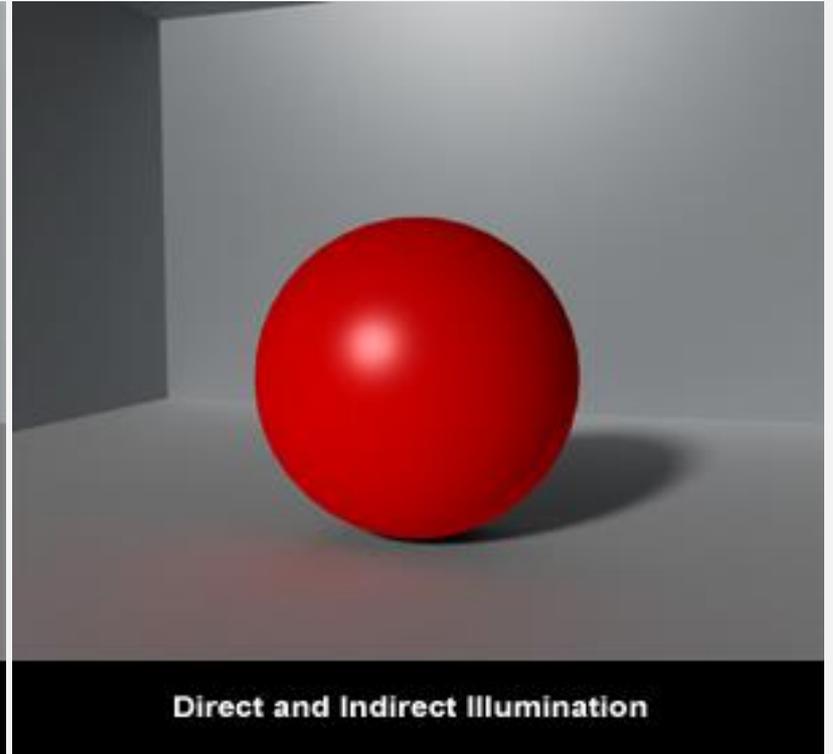
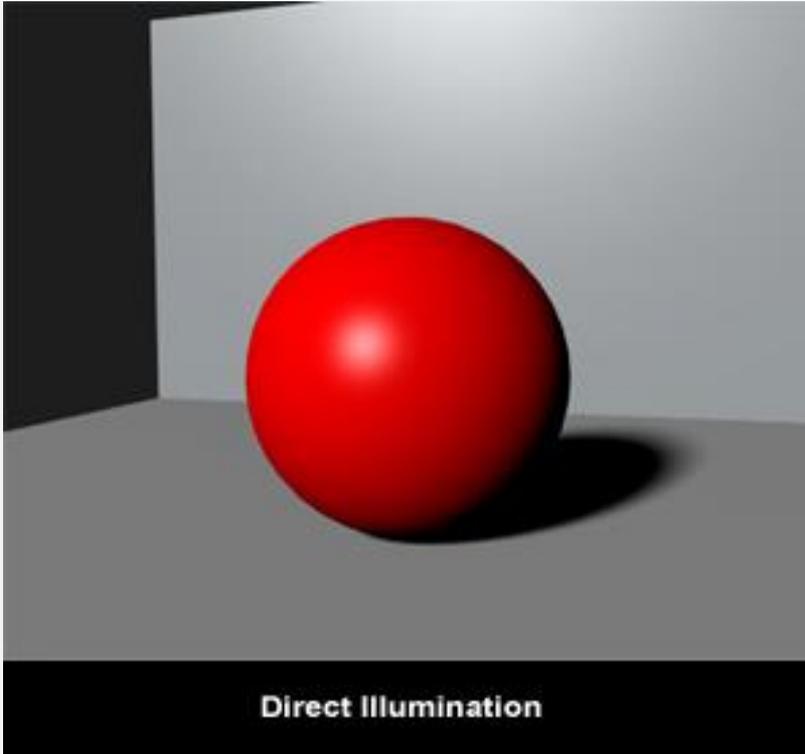
<http://hof.povray.org/>

# Radiosity



- Object hit by light is a new light source
- Energy (light) exchange between objects
- Indirect illumination

<http://www.bxhdesigns.com/>



# Real world radiosity



- Light reflectors in photography

<http://www.hootphotography.com>



Harsh Shadows



Silver reflector filling in light



# Radiosity

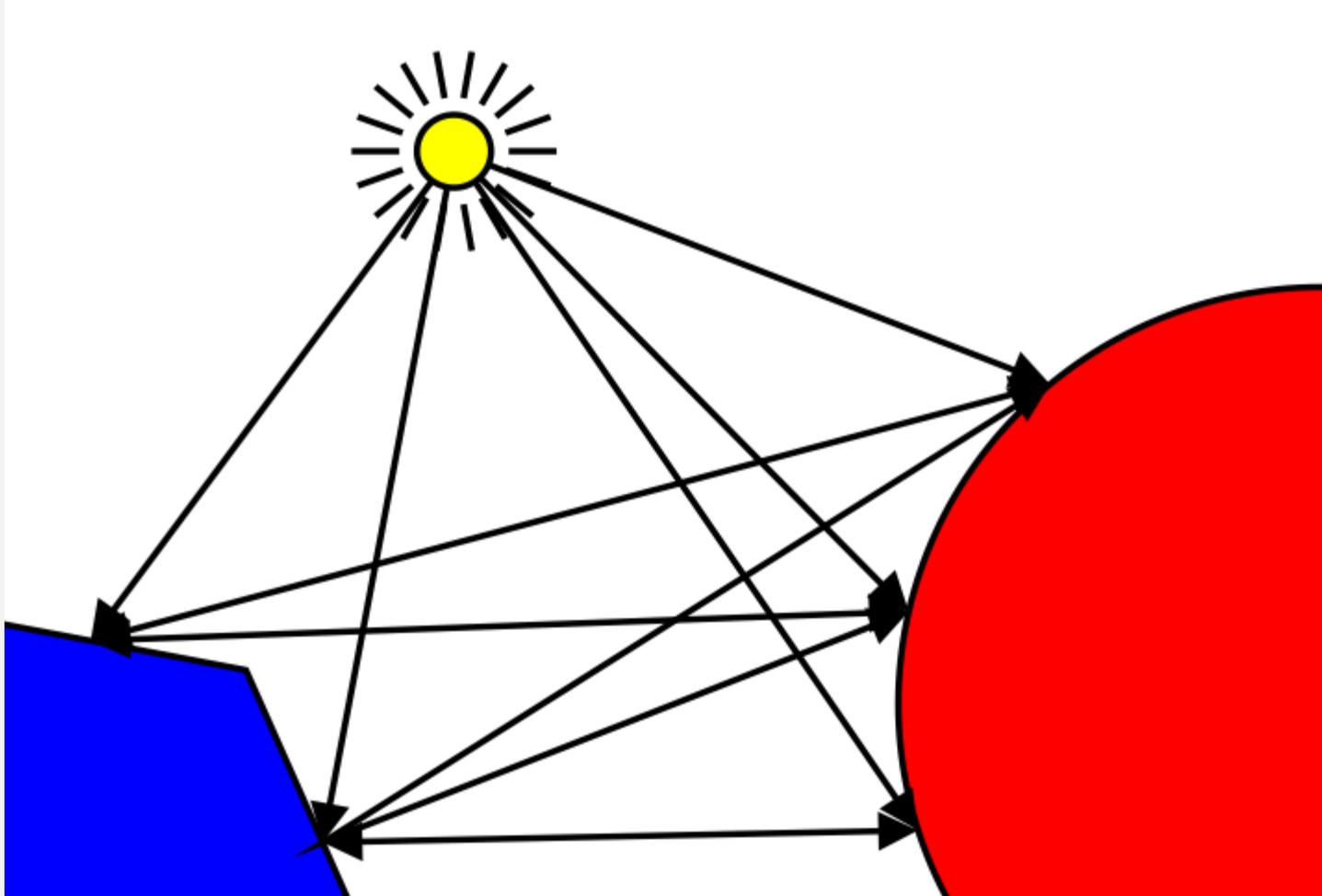


- Physically based
- Object hit by light becomes a new light source
- Not only object-light interaction
- But also object-object light interaction
- Energy exchange between objects



[http://www.ehow.com/video\\_4938383.html](http://www.ehow.com/video_4938383.html)

# General situation

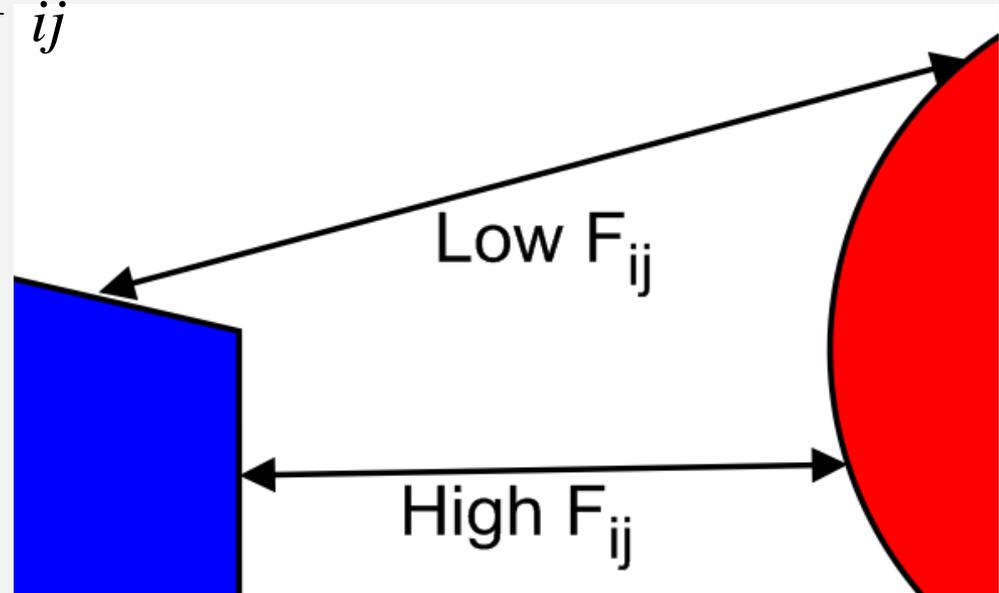


# The math behind it

- Energy is either emitted (E) or bounced (B)
- All reflections are perfectly diffuse
- Surface  $A_i$  radiosity:

$$B_i = E_i + \rho_i \sum_{\forall A_j} B_j F_{ij}$$

- Form factors  $F_{ij}$ 
  - how two surface elements  $A_i$  and  $A_j$  affect each other



# Elementary example

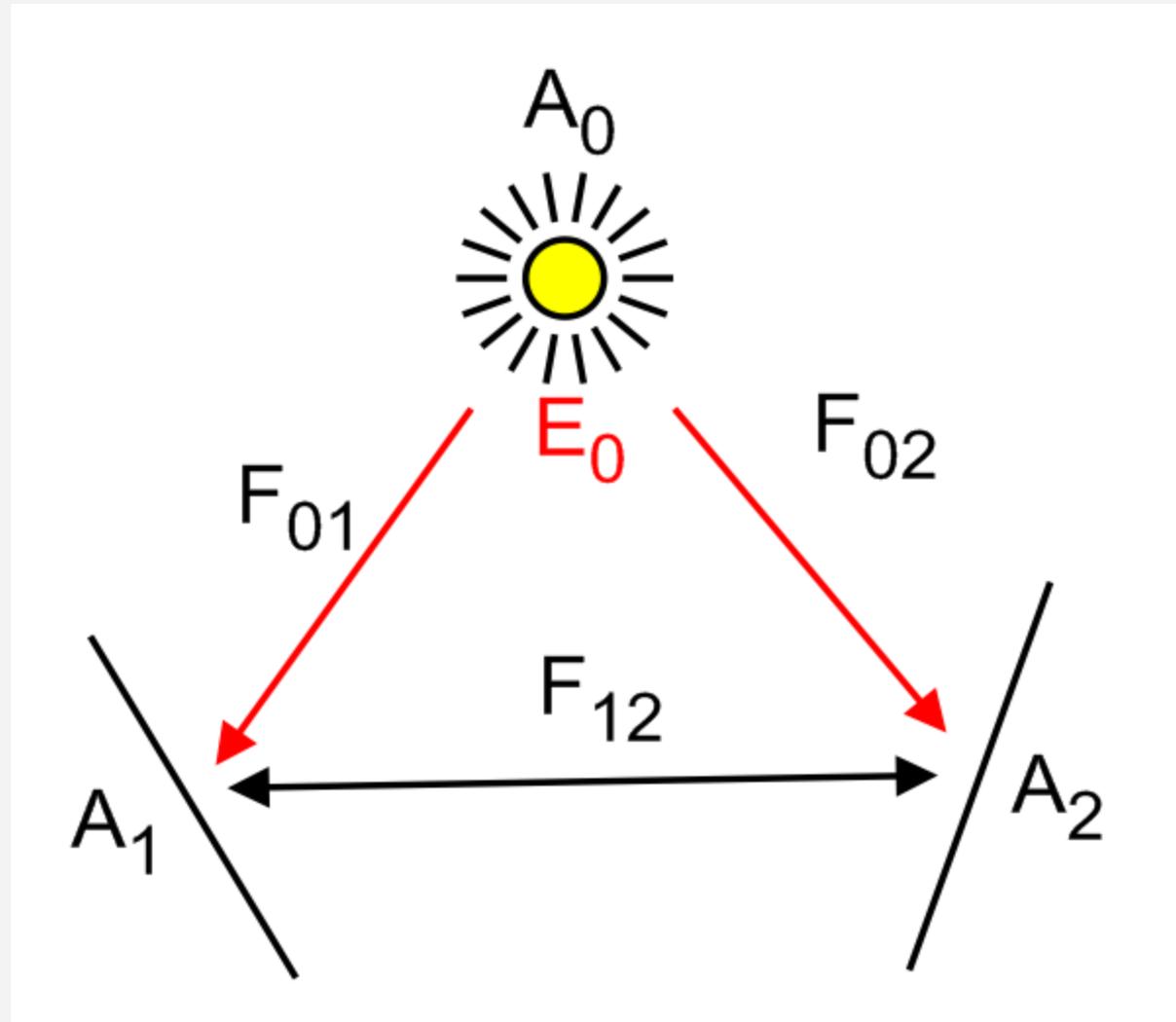


- Problem:

$$B_1 = ?$$

$$B_2 = ?$$

- Let  $E_1 = E_2 = 0$



# Energy preservation



- Bounced = Emitted + p\*Received

$$B_1 = E_1 + p_1(B_0F_{01} + B_1F_{11} + B_2F_{12})$$

$$B_1 - p_1(B_0F_{01} + B_1F_{11} + B_2F_{12}) = E_1$$

$$- p_1B_0F_{01} + B_1(1 - p_1F_{11}) - p_1B_2F_{12} = E_1$$

- Repeat for all 3 surfaces

# Result = linear system



$$\begin{pmatrix} 1 - p_0 F_{00} & -p_0 F_{01} & -p_0 F_{02} \\ -p_1 F_{10} & 1 - p_1 F_{11} & -p_1 F_{12} \\ -p_2 F_{20} & -p_2 F_{21} & 1 - p_2 F_{22} \end{pmatrix} \begin{pmatrix} B_0 \\ B_1 \\ B_2 \end{pmatrix} = \begin{pmatrix} E_0 \\ E_1 \\ E_2 \end{pmatrix}$$

- $E_1 = E_2 = 0$
- $E_0 =$  light source parameter
- In real – tens of thousands of surfaces

# Radiosity pros and cons

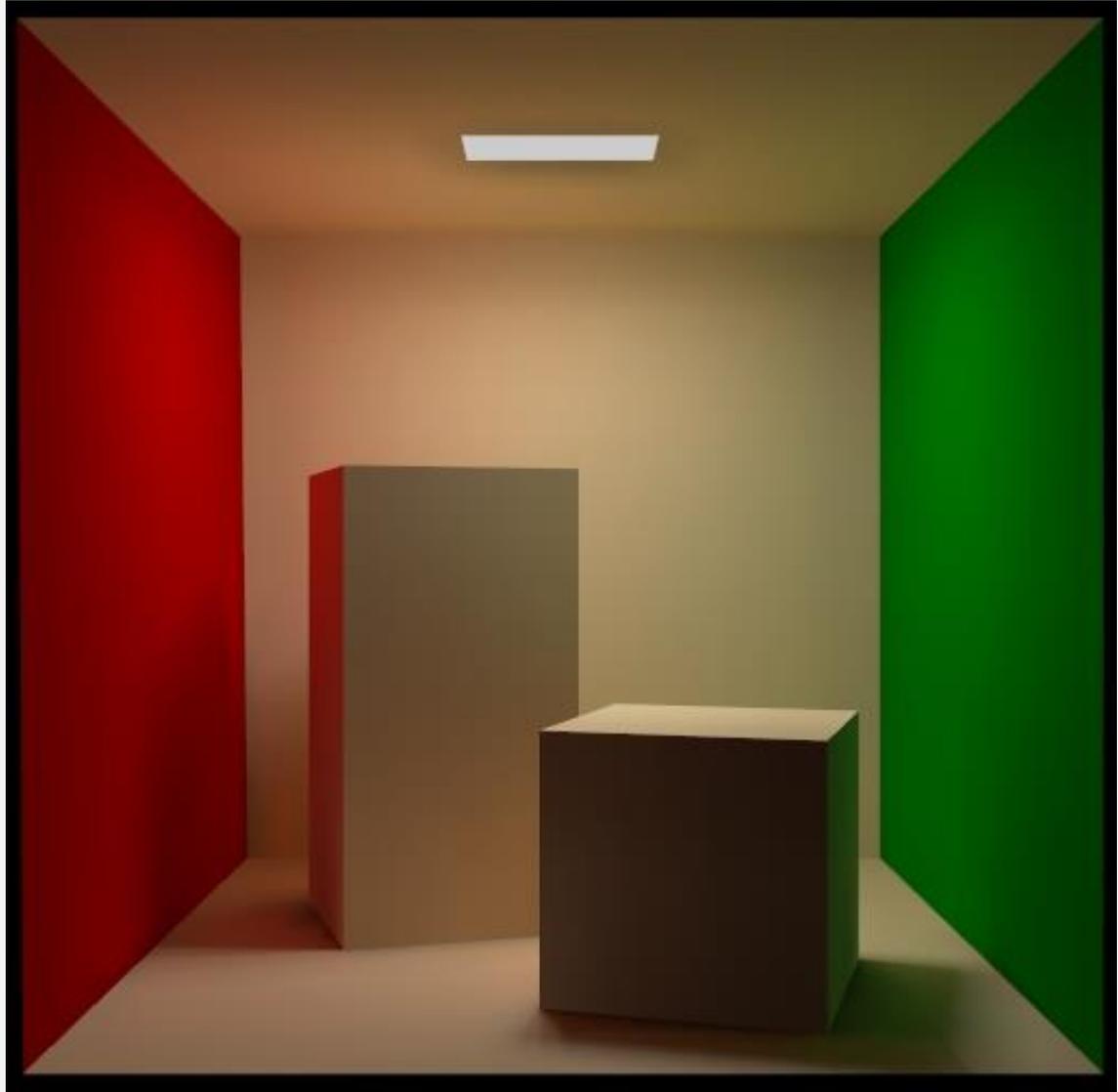


- Physically correct
- Extreme computational expenses
- Indirect light
  - soft realistic shadows
- Area lights and object lights are easy to do
- Color bleeding possible too
- Only diffuse light transfer = Problems with reflections and specular light

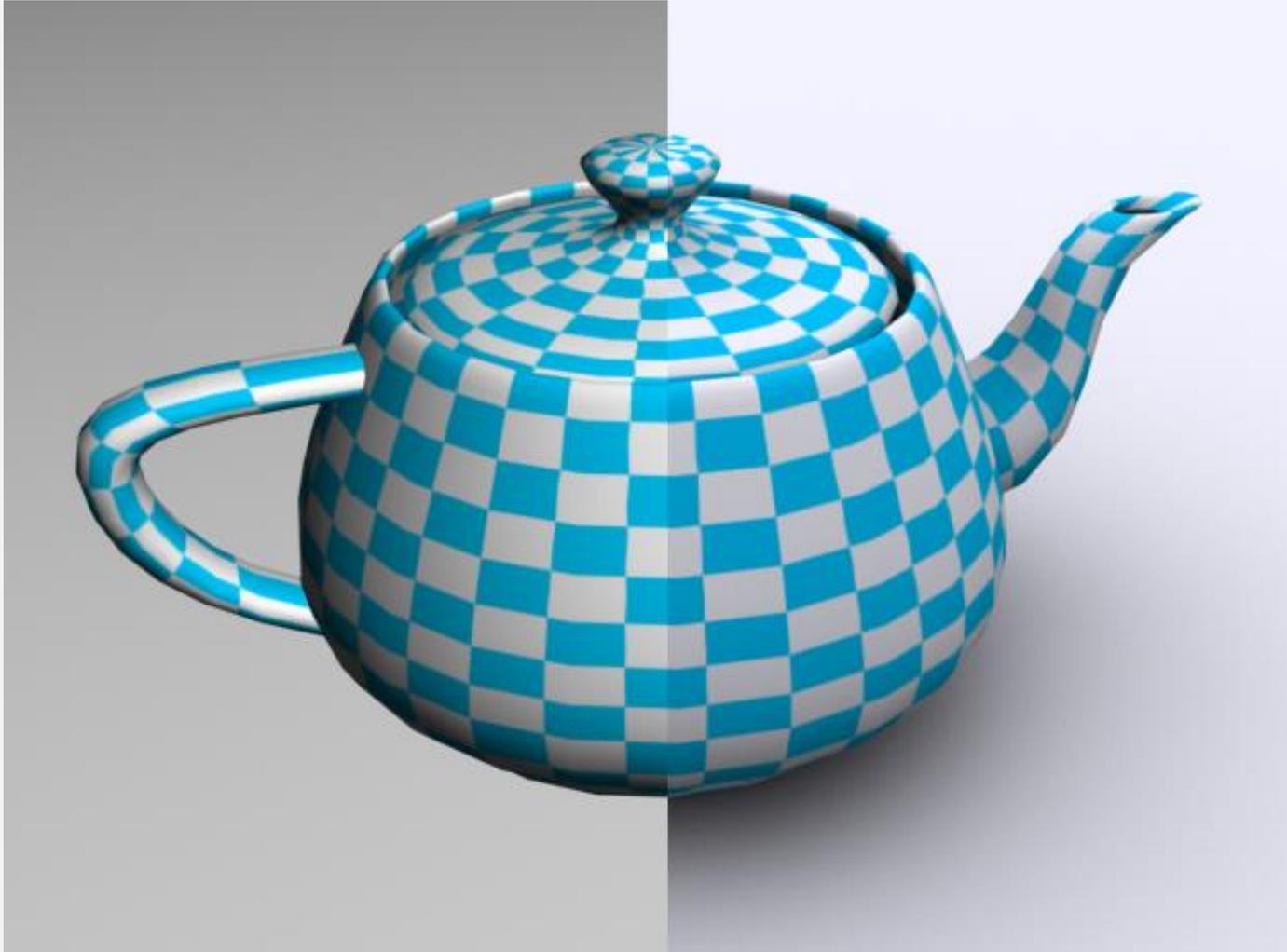
# Example



- Indirect light
- Color bleeding
- Soft shadows
- Area light



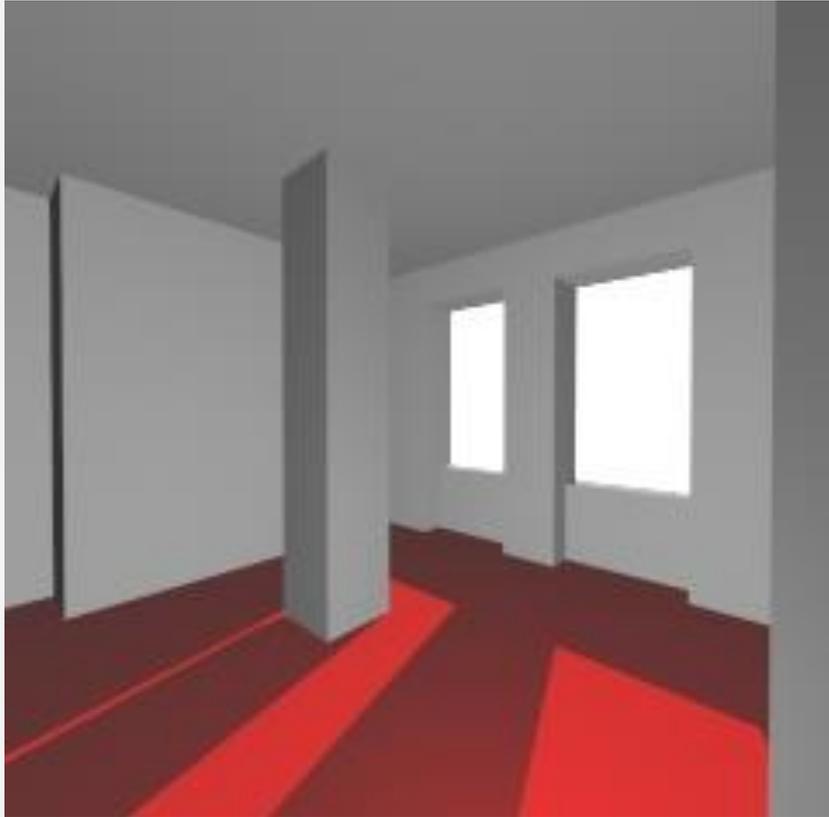
# Radiosity example



direct illumination

indirect illumination

# Raytracing vs. radiosity



<http://www.soe.ucsc.edu/classes/cms161/Winter04/projects/aames/index.htm>



Questions?